

# The evolution of H II galaxies: testing the bursting scenario through the use of self-consistent models

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## ABSTRACT

We have computed a series of realistic and self-consistent models of the emitted spectra of H II galaxies. Our models combine different codes of chemical evolution, evolutionary population synthesis and photoionization. The emitted spectrum of H II galaxies is reproduced by means of the photoionization code CLOUDY, using as ionizing spectrum the spectral energy distribution of the modelled H II galaxy, which in turn is calculated according to a star formation history and a metallicity evolution given by a chemical evolution model that follows the abundances of 15 different elements. The contribution of emission lines to the broad-band colours is explicitly taken into account.

The results of our code are compared with photometric and spectroscopic data of H II galaxies. Our technique reproduces observed diagnostic diagrams, abundances, equivalent width–colour and equivalent width–metallicity relations for local H II galaxies.

**Key words:** galaxies: abundances – galaxies: evolution – galaxies: starburst – galaxies: stellar content.

## 1 INTRODUCTION

H II galaxies, a subset of blue compact galaxies (BCG), are gas-rich dwarf galaxies whose optical spectra are dominated by strong and narrow emission lines. They are currently experiencing intense star formation in small volumes. The emission lines are produced by gas ionized by the young massive stars. Observations indicate that H II galaxies are in general metal-poor systems. This fact in addition to their very young stellar populations has been known for some time and has led to the proposal that these systems are very young, suffering their first burst of star formation (Sargent & Searle 1970).

It seems, however, that these galaxies are not as young as it was originally thought, since recent photometric observations indicate that they host stellar populations which are at least  $10^7$ – $10^8$  a old, reaching in some cases a few Ga (Telles, Melnick & Terlevich 1997; Legrand 2000; Cairós et al. 2003; Tolstoy 2003; van Zee, Barton & Skillman 2004; Thuan & Izotov 2005). There is now wide agreement about the existence of underlying populations with ages of several Ga in BCGs and/or H II galaxies. Even in the most metal-poor galaxy known, Izw18, the best candidate to *primordial galaxy*, there is an underlying population of at least some  $10^8$ – $10^9$  a (Izotov & Thuan 2004).

However, there is no consensus about their history of star formation. Two scenarios are postulated as follows:

(i) The star formation takes place in short but intense episodes separated by long quiescent periods of null or low activity (Bradamante, Matteucci & D’Ercole 1998).

(ii) The star formation is continuous and of low intensity along the galaxy life, with superimposed sporadic bursts (Legrand 2000).

In both scenarios, a stellar population of intermediate age contributes to the observed luminosity. Indeed, recent work takes into account the existence of an underlying stellar population and combine photoionization codes with evolutionary synthesis models (hereinafter ESMs). Examples of this procedure can be found in Garnett et al. (1999), Mas-Hesse & Kunth (1999), Stasińska & Izotov (2003) and Moy, Rocca-Volmerange & Fioc (2001). In general the ESMs so far do not include the chemical evolution. Given the low metal content of H II galaxies the metallicity effect can be of considerable relevance.

Terlevich et al. (2004) have shown that the equivalent width of the H $\beta$  line, EW(H $\beta$ ), which can be taken as an age indicator for the ionizing population, and the ( $U - V$ ) colour in H II galaxies show an anticorrelation which cannot be interpreted in terms of a single stellar population (SSP). At a given EW(H $\beta$ ) the data are displaced to colours redder than those predicted by the models. The most likely explanation is that the ionizing population, which is the most recent burst of star formation, is overimposed on an older stellar population evolved enough as to produce a redder ( $U - V$ ) colour. There is also an inverse correlation between EW(H $\beta$ ) and the gas oxygen abundance,  $12 + \log(O/H)$ , which could be interpreted

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in terms of galactic chemical evolution: as the average age and the total mass of the stellar population increases, the  $EW(H\beta)$  decreases and the mean metallicity of the interstellar medium (ISM) increases.

A number of works (Shi, Kong & Cheng 2006 and references therein) have computed purely chemical evolution models (hereinafter CEMs) for the study of BCG and dwarf irregular galaxies. Most of them assume that the star formation occurs in bursts and include the effects of galactic winds and/or gas infall. However, most of them limit the study to the evolution of nitrogen and oxygen abundances (Henry, Edmunds & Köppen 2000; Larsen, Sommer-Larsen & Pagel 2001) and/or the luminosity–metallicity relation (Mouhcine & Contini 2002). Only Vázquez, Carigi & González (2003) used the information coming from the CEMs from Carigi, Hernandez & Gilmore (2002) to perform the next step and combine chemical and spectral evolution. Their models exclude however the early stages of evolution, i.e. during the nebular stage when the most massive stars dominate the energy output.

A code combining chemical evolution, evolutionary synthesis and photoionization models has not yet been developed and used for the spectral analysis of BCG and H II galaxies.

In this work, we include the CEM results in the computation of the spectral energy distributions (SEDs) which are used as ionizing source for a photoionization code.

Our method allows the simultaneous use of the whole available information for the galaxy sample concerning on the one hand the ionized gas – emission lines intensities and EWs, elemental abundances, gas densities – which defines the present time-state of the galaxy, and on the other hand spectrophotometric parameters – colours, absorption spectral indices – defined by the stellar populations and their evolution with time and thus related to the galaxy star formation history (SFH). This is done in a self-consistent way, i.e. using the same assumptions regarding stellar evolution, model stellar atmospheres and nucleosynthesis, and using a realistic age–metallicity relation.

The basic codes employed are described in Section 2. Section 3 shows the corresponding results of each kind of model, and the whole combined results about galaxy evolution. These results are discussed in Section 4. Finally, our conclusions are summarized in Section 5.

## 2 MODEL DESCRIPTION

### 2.1 Chemical evolution

The code used for this work is a generalization of the code used for the solar neighbourhood by Ferrini et al. (1992) and applied to the whole Galaxy disc in Ferrini et al. (1994). That model described the galaxy as a two-zone system (halo and disc) in which the disc is a secondary structure formed by the gravitational accumulation of gas from the halo. In the present work, however, all the gas is assumed to be within an only region from  $t = 0$ , i.e. the collapse time-scale has been eliminated as an input parameter of the code. The matter is assumed to be in different phases.

(i) A stellar population, where we distinguish the stars able to create and eject heavy elements to the ISM ( $M > 4 M_{\odot}$ ), and the stars which only eject hydrogen and He ( $M < 4 M_{\odot}$ ).

(ii) Stellar remnants, as the endpoint of star evolution, that act as a matter sink, removing mass from chemical evolution.

(iii) Interstellar diffuse gas out of which stars are forming following a simple Schmidt law. No molecular component is explicitly considered in the present work.

A bursting star formation has been assumed taking place in successive bursts along the time evolution. At any time, the available gas for each burst is the sum of the gas left after the previous burst of star formation and the gas ejected by massive stars.

According to this description, the time dependence of the total mass fraction in each phase and the chemical abundances in the ISM are determined by the interactions between these phases and, as a consequence of the evolution, we get the star formation rate. The basic equations to study the behaviour of the mass of stars and gas are, therefore

$$\frac{dM}{dt} = 0, \quad (1)$$

$$\frac{dM_s}{dt} = \Psi - E, \quad (2)$$

$$\frac{dM_g}{dt} = -\Psi + E, \quad (3)$$

$$M = M_s + M_g, \quad (4)$$

where  $M_s(t)$  is the mass in stars,  $M_g(t)$  is the mass of gas,  $M$  is the total mass of the system,  $\Psi(t)$  the star formation rate and  $E(t)$  the ejection rate of mass from the stars to the ISM. A part of the restituted gas consists of enriched material,  $E_Z(t)$ , which is created in the interior of the stars and is ejected when they die. To compute both quantities, ejected gas and element production, we use the  $Q_{ij}$  matrix formalism introduced by Talbot & Arnett (1973) and widely used in classical CEMs. It is very useful to treat elemental abundances which increase at different rate in the ISM, i.e. the non-solar elemental ratios (Portinari, Chiosi & Bressan 1998). In the present work we adopt the same matrix prescription as in Gavilán, Mollá & Buell (2006), which is an updated version from the one given in Ferrini et al. (1992) and Galli et al. (1995) calculated following the method described by Portinari et al. (1998).

In order to calculate these matrices it is necessary to consider the nucleosynthesis of stars, their initial mass function (IMF) and their end either as type I (SNe I) or II (SNe II) supernovae, or through quiet evolution. The mean stellar lifetimes, final states, and nucleosynthesis products, depend on the stellar mass which makes the IMF to play an important role in the CEM. The adopted IMF is assumed to be universal in space and constant in time (Wyse 1997; Scalo 1998; Meyer et al. 2000) and taken from Ferrini, Penco & Palla (1990). This IMF is very similar to Scalo’s law (Scalo 1986) and in good agreement with the recent expressions from Kroupa (2001) and Chabrier (2003). Nucleosynthesis yields for massive stars have been taken from Woosley & Weaver (1995). For low- and intermediate-mass stars, we have used the yields from Gavilán, Buell & Mollá (2005). The combination of these sets of stellar yields, with our assumed IMF producing the required yields per stellar generation, has been completely revised and calibrated with the Milky Way galaxy in Gavilán et al. (2005, 2006), where other stellar yields sets have been used and analysed too. It also reproduces observations of spiral and irregular galaxies (Mollá & Díaz 2005), obtaining reasonable results even for nitrogen abundances in low-metallicity objects (Mollá et al. 2006). For SN I explosion releases, model W7 from Nomoto, Thielemann & Yokoi (1984), as revised by Iwamoto et al. (1999), has been taken, while the rate of this type of SN Ia explosions are included through a table given by Ruiz-Lapuente (private communication), following works of Ruiz-Lapuente et al. (2000).

We have assumed that the gas is used to form stars with a given efficiency called  $H$ :  $\Psi = HM_g$ . If there would not be gas ejection

from massive stars, as it would be the case for instance in the first moments of the evolution, ( $E = 0$ ), then

$$\frac{dM_s}{dt} = HM_g, \quad (5)$$

$$\frac{dM_g}{dt} = -HM_g. \quad (6)$$

That is, the consumed gas rate would be a function that depends on the available gas at a given time,<sup>1</sup> being a decreasing function of time through the parameter  $H$ , which defines the star formation efficiency. Then

$$\frac{dM_g}{M_g} = -H dt \Rightarrow M_g(t) = M_{g,0} e^{-Ht}. \quad (7)$$

A change in the star formation rate implies a change in the value of the parameter  $H$  or efficiency

$$H = \frac{\ln(M_{g,0}/M_g)}{\Delta t}. \quad (8)$$

We have run models considering the star formation as a set of successive bursts in a region with a total mass of gas of  $100 \times 10^6 M_\odot$  and a radius of 500 pc (see Section 3.2 for details). Every galaxy experiences 11 star formation bursts along its evolution of 13.2 Ga, i.e. one every 1.3 Ga. In each burst a certain amount of gas is consumed to form stars. We have computed two types of models. In the first one, which we call *burst* models (models B), the same efficiency  $H$  is assumed for every burst while in the second one (models A) we assume an attenuated bursting star formation mode, i.e. a variable  $H$  is assumed along the time evolution. For each type we have computed two models with different initial star formation efficiency:

- (i) Model 1, which uses  $\sim 64$  per cent of the gas for star formation in each time-step. Thus, following equation (8),  $1/H = 0.5$  Ma.
- (ii) Model 2, which uses  $\sim 33$  per cent of the gas to form stars in each time-step, which implies  $1/H = 1.25$  Ma.

These percentages are maintained in models B, which means that every burst will transform the corresponding percentage of the available gas (taking into account the gas ejected by massive stars) in stars. In models A, these values correspond to the initial efficiencies and are reduced in the successive bursts by a factor  $n$ , where  $n$  is the number of the burst.

The code solves the chemical evolution equations to obtain, in each time-step, the abundances of 15 elements: H, D,  $^3\text{He}$ ,  $^4\text{He}$ , C,  $^{13}\text{C}$ , O, N, Ne, Mg, Si, S, Ca, Fe and  $nr$  where  $nr$  are the isotopes of the neutron-rich elements, synthesized from  $^{12}\text{C}$ ,  $^{13}\text{C}$ ,  $^{14}\text{N}$  and  $^{16}\text{O}$  inside the CO core. We have taken a time-step,  $\Delta t = 0.5$  Ma,<sup>2</sup> from the initial time,  $t = 0$ , up to the final one,  $t = 13.2$  Ga. Also, at each time-step, the star formation rate and the mass in each phase – low-mass, massive stars and remnants, total mass in stars created and mass of gas – are computed. This amounts to a total of 26 348 stellar *generations* or SSPs, each one with its corresponding age and metallicity.

## 2.2 Evolutionary synthesis

Once the CEMs have been calculated, the spectrophotometric properties can also be obtained. In this work we have used the code from

García-Vargas, Bressan & Díaz (1995a,b) and García-Vargas, Mollá & Bressan (1998) as updated in Mollá & García-Vargas (2000). The required inputs are the stellar isochrones and the stellar atmosphere models for the individual stars. In that work we used the set of 50 isochrones from the Padova group from Bertelli et al. (1994) for ages between 4 Ma and 20 Ga, for five metallicities between  $1/50$  and  $2.5 Z_\odot$  ( $Z = 0.0004, 0.004, 0.008, 0.02$  and  $0.05$ ). To this set of isochrones we have added other 18 isochrones from Bressan et al. (1993) and Fagotto et al. (1994a) with ages from 0.5 to 4 Ma, used in García-Vargas et al. (1995a) and García-Vargas et al. (1998) for the youngest stellar populations of four metallicities  $Z = 0.004, 0.008, 0.02$  and  $0.05$ . That means that for the lowest metallicity,  $Z = 0.0004$ , only isochrones older than 4 Ma are available.

In both cases, isochrones give the number of stars in each phase assuming that stellar clusters were formed with a standard Salpeter IMF with  $m_{\text{low}} = 0.6 M_\odot$  and  $m_{\text{up}} = 100 M_\odot$ . This IMF, although using the same lower and upper limits, is not exactly the one used in the multiphase chemical evolution code, which implies some differences in the resulting spectra, mainly for the oldest and the youngest stellar populations. They are, however, smaller than 10 per cent (García-Vargas et al., in preparation), and therefore we assume that this inconsistency will not produce very important differences in the final results.

The emergent SED was synthesized by calculating the number of stars in each point of the Hertzsprung–Russell diagram and assigning to it the most adequate stellar atmosphere model. The models of Clegg & Middlemass (1987) and Lejeune, Cuisinier & Buser (1997) have been used for stars with  $T_{\text{eff}} \geq 50\,000$  K (last evolutionary stages of massive stars) and  $2500 \leq T_{\text{eff}} < 50\,000$  K, respectively.

To each SED computed for a stellar cluster, it was added a continuum nebular emission contribution as explained in García-Vargas et al. (1998). The gas is assumed to have an electron temperature,  $T_e$  which depends on  $Z$ . The assumed values are  $T_e = 18\,000, 11\,000, 9000, 6500$  and  $4000$  K for  $Z = 0.0004, 0.004, 0.008, 0.02$  and  $0.05$ , respectively, selected according to the average value obtained by García-Vargas et al. (1995b). The free–free, free–bound emission by hydrogen and neutral helium, and the two photon hydrogen-continuum have been calculated by means of the atomic data from Aller (1984) and Ferland (1980).

The SEDs for the complete sets of 68 (50 for  $Z = 0.0004$ ) isochrones were calculated with the same code as in Mollá & García-Vargas (2000)<sup>3</sup> for the cited metallicities. Therefore we finally have a set of 68 SEDs for SSP of different ages for four metallicities each, and 50 for ages older than 4 Ma for  $Z = 0.0004$ , which we use as a spectral library.

Once the SEDs for SSPs are computed, they must be convolved with the SFH in order to calculate the corresponding SED for a region where more than a burst take place:

$$L_\lambda(t) = \int_0^t S_\lambda(\tau, Z(t')) \Psi(t') dt', \quad (9)$$

where  $\tau = t - t'$  is the age of the stellar population created in a time  $t'$  and  $S_\lambda$  being the SED for each SSP of age  $\tau$  and metallicity  $Z$  reached in that time  $t'$ . An SED from the SSP library,  $S_\lambda$ , must be assigned to each time-step according to its corresponding age and metallicity taking into account the SFH,  $\Psi(t)$ , and the age–metallicity relation,  $Z(t)$ , obtained from the CEM, to finally calculate  $L_\lambda(t)$  by the

<sup>1</sup> When  $E \neq 0$  this expression is modified, as we will show in Section 3.

<sup>2</sup> This small time-step allows to take into account the fast evolutionary phases of the most massive stars considered.

<sup>3</sup> Although in that work, applied to old elliptical galaxies, the SEDs corresponding to ages younger than 4 Ma and those for  $Z = 0.0004$ , were not used.

above integration. However, the metallicity changes continuously while the available SEDs have only four or five possible values. We have, therefore, interpolated logarithmically between the two SSP of the same age  $\tau$  closest in metallicities to  $Z(t')$  to obtain the corresponding  $S_\lambda(\tau, Z(t'))$ . The final result is the total luminosity at each wavelength  $\lambda$ .

When this process is applied to the stellar population created by the first burst two problems arise. On the one hand the initial metallicity is  $Z = 0$  and, although during the first Ma after the creation of the first stars the metallicity increases, it does not reach the minimum  $Z = 0.0004$ , and therefore we must extrapolate with the available SEDs of the youngest SSPs. Due to the uncertainties in the evolution of the *quasi-zero-metallicity* stars, we have preferred to assign to this first burst metallicity a minimum value of 0.0028, smaller than the one reached at the end of the first burst but still valid for extrapolating without creating instability numerical problems. On the other hand we must use two different pairs of metallicities to extrapolate with the SEDs of SSPs:  $Z = 0.004$  and 0.008 before 4 Ma and  $Z = 0.0004$  and 0.004 after 4 Ma, since SEDs for the most metal-poor and youngest SSPs are not available. We have checked that this method does not produce discontinuities and that the resulting spectra behave smoothly. In this way we obtain the SED corresponding to the whole stellar population, including the ionizing continuum proceeding from the last formed stellar population.

### 2.3 Photoionization

The photoionization code CLOUDY, in its 96.0 version (Ferland et al. 1998), has been used in order to obtain the emission lines. The gas is assumed to be ionized by the massive stars belonging to the current burst of star formation whose SED has been previously calculated by the combination of the chemical and ESMs. The shape of the ionizing continuum is defined by the pair of values ( $\nu(\text{Ryd})$ ,  $\log \nu L_\nu$ ) (equation (9)).

We have assumed the emitting gas to be located at a distance  $R = 500$  pc at the beginning of the evolution. This size is characteristic of H II galaxies (Telles et al. 1997). This radius is subsequently adjusted as to keep a constant stellar density configuration. This results in all cases in a plane-parallel geometry.

A given model is characterized by its ionization parameter  $U$  defined as

$$U = Q(H)/4\pi cn_{\text{H}}R^2, \quad (10)$$

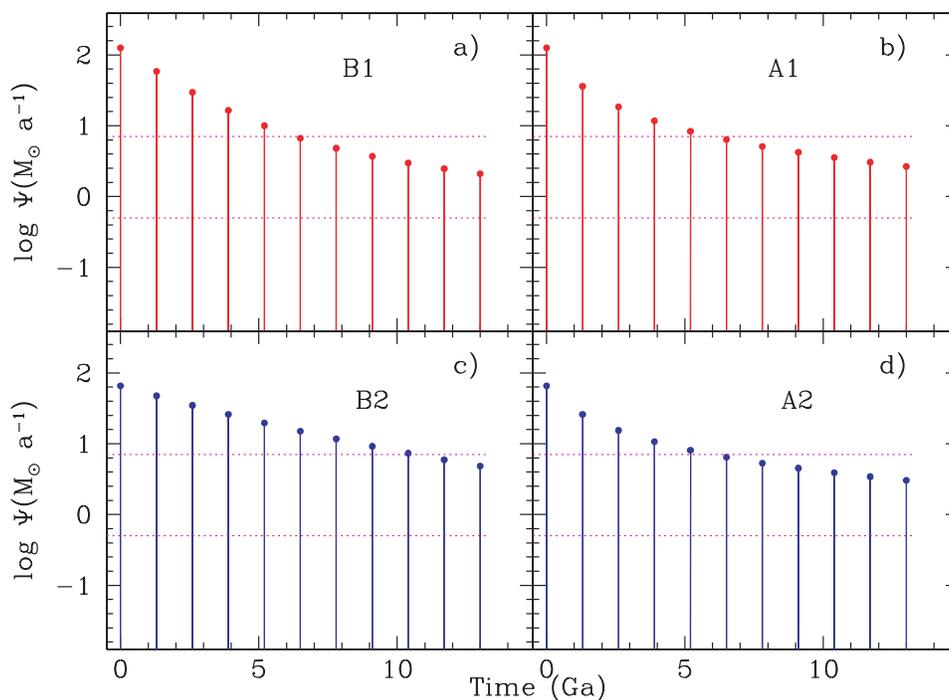
where  $n_e$  is the electron density, assumed constant for simplicity and equal to  $100 \text{ cm}^{-3}$ , and  $Q(H)$  is the number of Lyman ionizing photons, calculated from the cluster SED, which reach the gas at a velocity  $c$ . Finally, the gas elemental abundances are those reached at the end of the starburst previous to the current one, as calculated from the CEM, except for Na, Ar and Ni which are not computed in the model and are scaled to the solar ratio (Asplund, Grevesse & Sauval 2005).

## 3 RESULTS

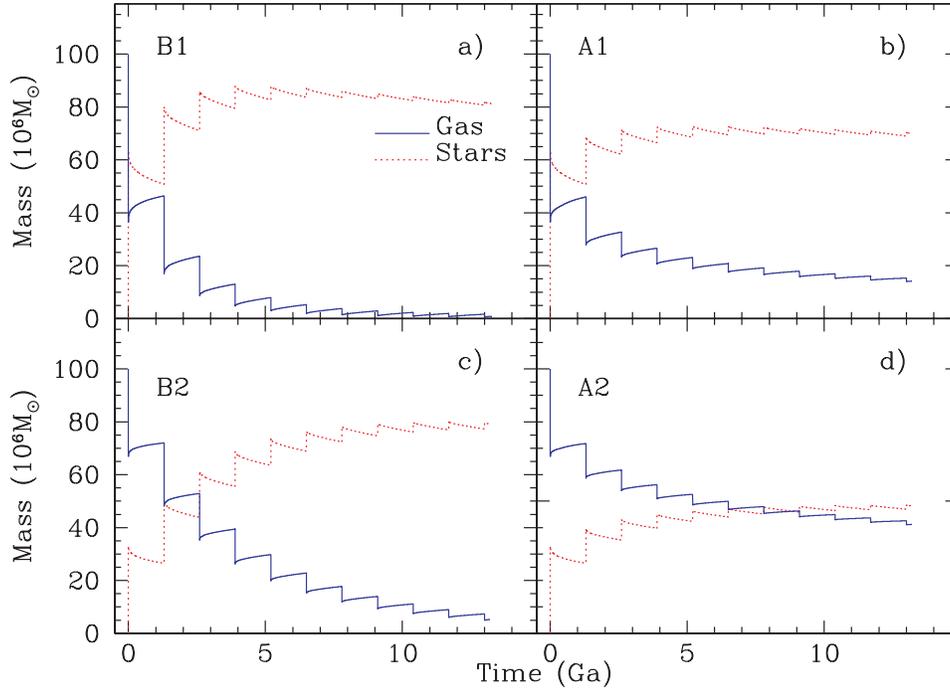
### 3.1 Chemical evolution

#### 3.1.1 Star formation rates

The star formation rate is one of the main results of the different models since it drives the behaviour of all the other quantities. In Fig. 1 the SFH for each of the four computed models is shown. In all of them the first burst is strong, while the successive bursts are less intense since the amount of gas available has decreased in spite of the ejected gas produced by the massive stars. In models A (right-hand panels), the first burst has the same star formation rate as in models B (left-hand panels), since the initial efficiency is the same for both. The successive star formation episodes have a smaller star



**Figure 1.** SFH for (a) burst model 1 (B1); (b) attenuated burst model 1 (A1); (c) burst model 2 (B2); and (d) attenuated burst model 2 (A2). Dotted lines represent the upper and lower limits to the SFR estimated for BCG and/or H II galaxies by Hoyos et al. (2004).



**Figure 2.** Time evolution of the gas and star mass for models: (a) B1; (b) A1; (c) B2 and (d) A2.

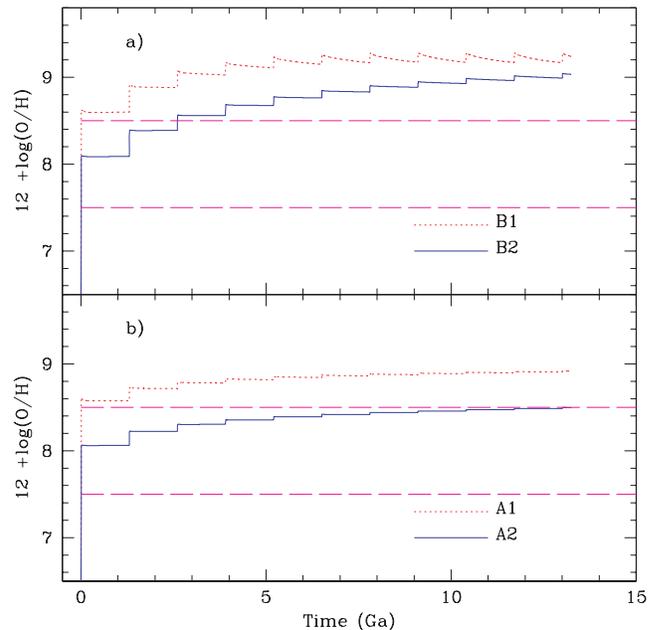
formation rate in models A than the corresponding ones in models B due to the attenuation factor included in the inputs.

Hoyos et al. (2004) have estimated the star formation rates for the sample of 39 local H II galaxies of different morphologies from Telles et al. (1997), which were selected from the most luminous of the Terlevich et al. (1991) catalogue and with H $\beta$  EWs between 30 and 280 Å. These star formation rates were obtained from the H $\alpha$  luminosity, by assuming  $T_e = 10^4$  K and case B recombination. They are in the range from 0.5 to  $7 M_\odot a^{-1}$ , marked by dotted lines in Fig. 1, indicating that these H II galaxies have high star formation rates. These findings are in agreement with those from Taylor et al. (1994) who found star formation rates in the range of  $10^{-4}$  to  $10 M_\odot a^{-1}$ . Our models produce SFR between the observed values after the sixth burst, which corresponds to 6.5 Ga after the beginning of star formation, except model B2, where every burst before the ninth–tenth show higher SFR than observed.

Since the star formation consumes gas, the averaged gas mass decreases with time following equation (6), as can be seen in Fig. 2. The chemical evolution code, however, takes into account the mass of gas ejected from massive stars during their evolution and, therefore, the gas mass increases during a given burst. On the other hand, the mass of stars which increases in each burst and globally due to the star formation, decreases during each burst as the most massive stars end their lives. It is interesting to note that models with smaller efficiencies,  $H$ , in the lower panels of Figs 1 and 2, consume less gas in each burst and, as a consequence, the star formation rate remains higher, and declines more slowly, than in models with higher values of  $H$  shown in the upper panels.

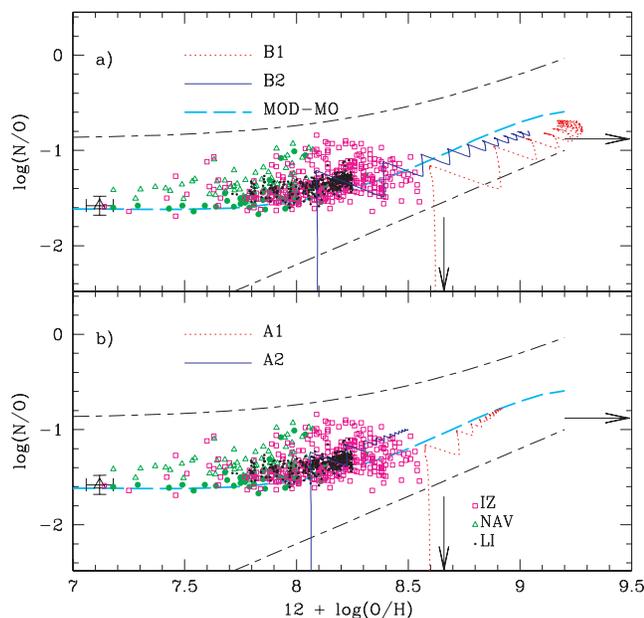
### 3.1.2 Elemental abundances

The element content of the gas is usually measured through the oxygen abundance, given as  $12 + \log(O/H)$ . Oxygen contributes more than 40 per cent to the mass in metals and is mainly created



**Figure 3.** Time evolution of the oxygen abundance, given as  $12 + \log(O/H)$ , for the four kinds of computed models: (a) models of type B (burst modes) and (b) models of type A (attenuated models) with dotted lines corresponding to models of type 1 and solid lines corresponding to models of type 2. The dashed lines limit the range of data taken from Terlevich et al. (1991) and Hoyos & Diaz (2006).

within massive stars. Since these stars are very short lived, their products are ejected very rapidly to the ISM and hence the value of its oxygen abundance increases with time, as shown in Fig. 3. In that figure we see how  $O/H$  increases abruptly when a burst takes places remaining more or less constant between each two of them.



**Figure 4.** The logarithmic N/O ratio as a function of the oxygen abundance, given as  $12 + \log(O/H)$ , for our four kinds of computed models: (a) type B models; (b) type A models. The (black) dashed lines limit the range of data shown by extragalactic H II regions. The (green) dots and (magenta) squares correspond to the derived values for low-metallicity galaxies from Izotov & Thuan (1999); Izotov et al. (2005); Hoyos & Díaz (2006); Izotov et al. (2006); Liang et al. (2006); Nava et al. (2006), while the large triangle is the value for the lowest metallicity galaxy in the sample SBS 0335–052W. The long-dashed (cyan) lines represents the averaged trend shown by CEMs from Mollá et al. (2006) for spiral and irregular galaxies with continuous star formation. The arrows mark the solar values.

Observational data from Terlevich et al. (1991) and Hoyos & Díaz (2006) show that most of the H II galaxies have metallicity distributions between  $7.5 < 12 + \log(O/H) < 8.5$ . These limits are shown as dashed lines in Fig. 3. The first limit is reached with the first burst in all cases. It can be seen that models of type 1 (dotted lines) show oxygen abundances higher than the observed upper limit. The efficiency of the first burst is so high that a large number of massive stars are formed, and hence the oxygen abundance reaches rather high values in a very short time. Also the oxygen abundance of model B2 reaches values higher than shown by data from the third burst onwards ( $12 + \log(O/H) > 8.5$ ). Only model A2 shows oxygen abundances within the range of H II galaxies during the whole evolution since the attenuation of the bursts keeps the star formation lower than in the other three cases. The star formation efficiency taken for model A2 results to be an upper limit for H II galaxies in oxygen abundances and it may reproduce the most metal-rich systems.

Abundance ratios also give information about the star formation process, essentially the time-scale or duration of the bursts, when the production of the elements involved takes place in stars in different mass ranges. This is the case for the N/O ratio. Oxygen is very quickly ejected by the most massive stars. Nitrogen, however, may be created in stars of all masses. Moreover, the production of nitrogen may take place in two ways: (1) the main process requires another element like carbon or oxygen, to synthesize N through the CNO cycle, thus N shows, at least in part, a secondary behaviour. In that case the N abundance has to be proportional to the initial abundance of heavy elements and hence the N/O ratio grows with

metallicity. There is, however, a proportion of Nitrogen which must have a primary origin, as suggested by the data in Fig. 4 (Izotov & Thuan 1999; Izotov, Thuan & Guseva 2005; Izotov et al. 2006) shown by (green) dots which exhibit a constant N/O ratio. Nitrogen may be produced by low- and intermediate-mass stars (Gavilán et al. 2006) and therefore its contribution may appear in the ISM a certain time after the massive stars have died. In fact, N grows more slowly than the oxygen abundance in the range  $7.6 < 12 + \log(O/H) < 8.2$ , which may be explained by this primary behaviour (see Mollá et al. 2006, for details). In Fig. 4 we can see the oscillating behaviour of the N/O ratio shown by our computed models due to the successive bursts of star formation followed by quiescent periods. At the beginning of a given burst, the N/O ratio decreases, as the O is created and ejected by the most massive stars in the burst; then it increases during the quiescent periods between bursts as the low- and intermediate-mass stars die and eject their synthesized nitrogen while the oxygen abundance remains constant.

According to the results of this section, model A2 is the one better reproducing the observations, since the total mass, the gas fraction, the star formation rate and the oxygen abundances are within the range shown by data. Therefore, from now onwards, in what regards the ionizing continuum and emission line properties only the A2 model will be analysed.

### 3.2 Evolutionary stellar population synthesis

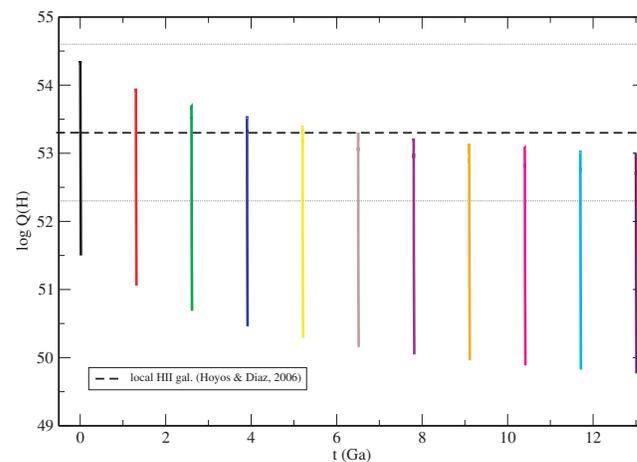
The convolution of the results of the chemical evolutionary code with the single stellar populations of the synthesis evolutionary code gives us directly the SED,  $L_\lambda$ , in time-steps of  $\log t = 0.05$ .

From this SED the number of hydrogen ionizing photons, coming from hot and young stars of the first spectral types ( $O - B$ ), can be calculated as

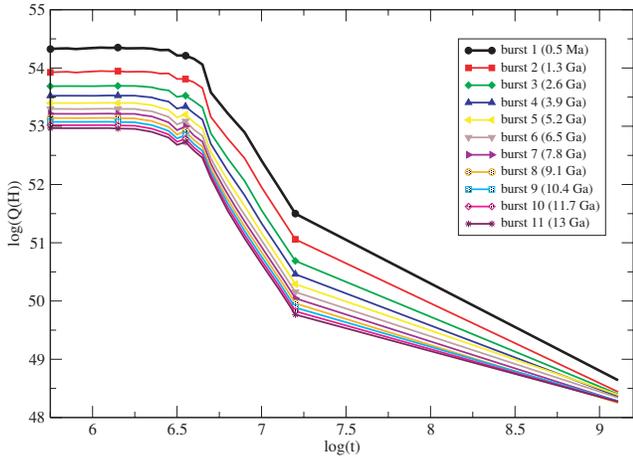
$$Q(H) = \int_{\nu_0}^{\infty} \frac{L_\nu}{h\nu} d\nu, \quad (11)$$

where  $L_\nu$  is the continuum luminosity at frequency  $\nu$ .

Fig. 5 shows the number of hydrogen ionizing photons as a function of time for model A2. In the first burst, with a total mass of  $\sim 30 \times 10^6 M_\odot$  forming stars, the number of massive ionizing stars is high and so it is the number of ionizing photons. The



**Figure 5.** The time evolution of the hydrogen ionizing photons,  $Q(H)$ , for model A2. The dotted line marks the mode of the distribution for local H II galaxies found by Hoyos & Díaz (2006). Each coloured line indicates the evolution within a burst. Different colour lines are used for different bursts.



**Figure 6.** The time evolution of the number of ionizing photons for each of the successive bursts during the 1.3-Ga interburst period. The burst number increases downwards. Different colour lines are used for the different bursts.

number of ionizing photons per unit stellar mass in our models is  $\log(Q(H)/M_{\odot}) \sim 46.8$  at the starting of the first burst, corresponding to a zero-age stellar population of very low metallicity and then decreases as the cluster ages. This initial number of ionizing photons per unit stellar mass is almost the same for the successive bursts although, decreasing slightly as the abundance increases.

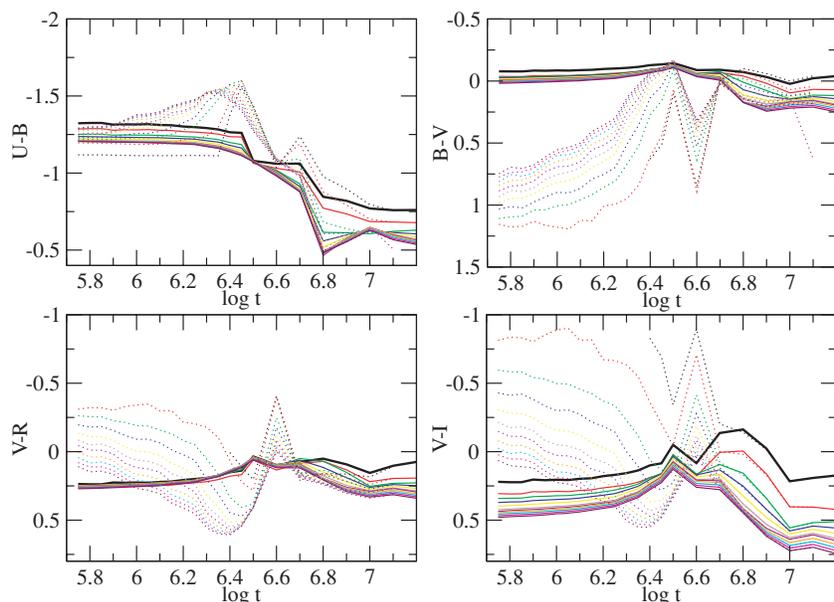
Within each burst the number of ionizing photons decreases by almost two orders of magnitude from 0.5 to 10 Ma, as show in Fig. 6, and by almost eight orders of magnitude by 100 Ma. Essentially no ionizing photons are available during the quiescent interburst periods. At the beginning of each successive burst, the number of ionizing photons rise abruptly but reach a value progressively lower as less gas is available to form stars. Also, as the mean gas metallicity increases with time, the number of ionizing photons per unit stellar mass decreases (García-Vargas et al. 1995a,b). This effect increases with the age of the ionizing cluster reaching a factor of about 5 at 10 Ma.

The average number of ionizing photons observed for local H II galaxies is  $\log(Q(H)) = 53.3$  (Hoyos & Díaz 2006). This number of ionizing photons, marked as a dotted line in Fig. 5, is reached by model A2 at around the fifth or sixth burst of star formation, that is for the burst occurring 5.2–6.5 Ga after the beginning of the formation of the galaxy, when the predicted star formation rate also fits the data (see Fig. 1). On the other hand, the average derived ionization parameter for the local H II galaxy sample is  $\log U = -2.5$  which in our models corresponds to an age of the ionizing population of about 6.5 Ma. It should be noted that during the first 7 Ma of a burst the number of ionizing photons remain essentially constant (see Fig. 6).

Therefore, if the current burst is identified with redshift  $z = 0$ , the formation of the galaxy would have taken place at a redshift  $z \sim 0.7$  (using  $H_0 = 74 \text{ km s}^{-1} \text{ Mpc}^{-1}$ , Macri et al. 2006). Also the observed number of ionizing photons for luminous compact blue galaxies (LCBGs) at a redshift  $0.46 < z < 0.7$ , estimated as  $\log(Q(H)) \sim 54.6$  (Hammer et al. 2001), would correspond to the value of the first burst of our models. According to these results, our model seems consistent with observations at these intermediate redshifts reproducing at the same time those corresponding to the more luminous local H II galaxies.

The question of if these galaxies are young galaxies, experiencing their first burst of star formation or if, on the contrary, there exists an underlying population formed some Ga ago, may be addressed by multicolour photometry. Although a direct detection of the underlying population in LCBG or H II galaxies is complicated because the observed light is dominated by massive stars, the effect of an underlying stellar population should be easily seen in the observed colours of these galaxies, since any star-forming burst previous to the currently observed one will contribute substantially to the total continuum luminosity at the different wavebands.

In Fig. 7 we represent the time evolution of the continuum  $U - B$ ,  $B - V$ ,  $V - R$  and  $V - I$  colours for our model A2 along the first 10 Ma after each burst. The first burst – solid black thick line – follows the expected evolution of a single stellar population of very low metallicity, remaining bluer than during the subsequent bursts where the effect of the accumulated continua from the previous star



**Figure 7.** Time evolution of colours for model A2: (a)  $U - B$ ; (b)  $B - V$ ; (c)  $V - R$ ; (d)  $V - I$ . The meaning of the (coloured) lines for different bursts is the same as in Fig. 5. Solid lines show the pure continuum colours while dotted lines also include the contribution by the strong emission lines.

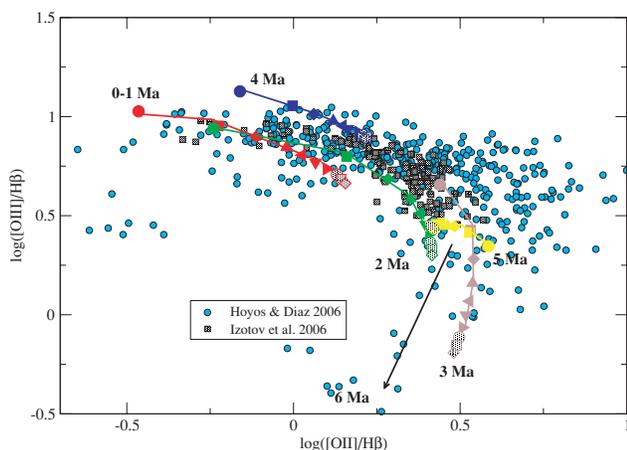
formation episodes makes colours become redder than expected for an SSP. Even though they are also starbursts in themselves, their star formation efficiency is much lower than that of the first burst, and so is their contribution to the total continuum luminosity which results in redder colours. Furthermore, the metallicity, almost zero for the first burst, increases up to  $Z = Z_{\odot}/5$  already during the second burst which also has an reddening effect over the colours.

### 3.3 Photoionization models

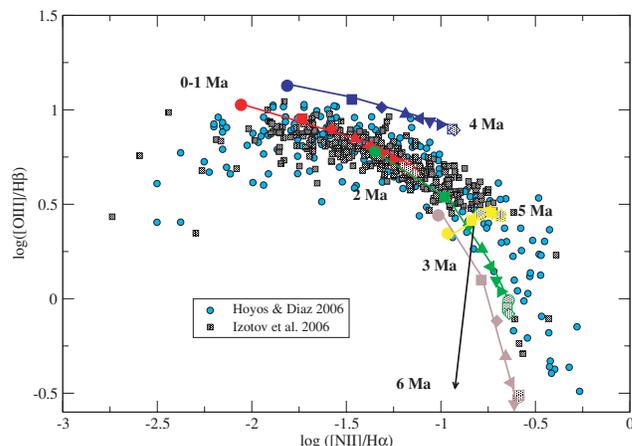
The calculated SED in each time-step can be used as input ionizing sources in the photoionization code to predict the emission lines intensities which provide information about the youngest stellar population which dominates the final spectra.

Fig. 8 shows the relation between the  $[\text{O III}]\lambda\lambda 4959, 5007/\text{H}\beta$  and  $[\text{O II}]\lambda\lambda 3727, 3729/\text{H}\beta$  ratios, which constitutes an excitation diagnostics for ionized nebulae. In this diagram, the most excited objects lie up and to the left-hand side while the objects with the lowest excitation are at the bottom right-hand side.

The data shown in the graph have been extracted mainly from two main sources. First, the compilation from Hoyos & Díaz (2006) which provides emission line measurements, corrected for extinction, published for local H II galaxies. The sample comprises 450 objects and constitutes a large sample of local H II galaxies with good-quality spectroscopic data. The sample is rather inhomogeneous in nature, since the data proceed from different instrumental set-ups, observing conditions and reduction procedures, but have been analysed in a uniform way. Data for these sample objects include the emission line intensities of  $[\text{O II}]\lambda\lambda 3727, 3729 \text{ \AA}$ ,  $[\text{O III}]\lambda\lambda 4959, 5007 \text{ \AA}$  and  $[\text{N II}]\lambda\lambda 6548, 6584 \text{ \AA}$ , all of them relative to  $\text{H}\beta$ , and the EWs of the  $[\text{O II}]$  and  $[\text{O III}]$  emission lines –  $\text{EW}([\text{O II}])$ ,  $\text{EW}([\text{O III}])$  – and the  $\text{H}\beta$  line,  $\text{EW}(\text{H}\beta)$ . As a second source, we have used the metal-poor galaxy data from the Data Release 3 of Sloan Digital Sky Survey (SDSS), taken from Izotov et al. (2006). The SDSS (York et al. 2000) constitutes a large data base of galaxies with well-defined



**Figure 8.** The relation between the oxygen line ratios for model A2. Solid coloured lines join the values reached at the same age by each different burst. Red, green, brown, blue and yellow colours correspond to ages 0–1, 2, 3, 4 and 5 Ma, respectively. Different bursts, except the first one, are represented by different symbols: solid circles, squares, diamonds, triangles up, triangles left, triangles down and triangles right correspond to bursts at 1.3, 2.6, 3.9, 5.2, 6.5, 7.8 and 9.1 Ga, respectively. Open circles, squares and diamonds correspond to bursts at 10.4, 11.7 and 13.2 Ga, respectively. The data are from references cited in the text.



**Figure 9.** The relation between the excitation parameter,  $\log([\text{O III}]/\text{H}\beta)$ , and the metallicity indicator  $\log([\text{N II}]/\text{H}\alpha)$  for model A2. The meaning of colours, symbols and lines is the same as in Fig. 8.

selection criteria and observed in a homogeneous way. The SDSS DR3 Abazajian et al. (2005) provides spectra in the wavelength range from 3800 to 9300  $\text{\AA}$  for  $\sim 530\,000$  galaxies, quasars and stars. Izotov et al. (2006) extracted  $\sim 2700$  spectra of non-active galaxies with the  $[\text{O III}]\lambda 4363 \text{ \AA}$  emission detected above  $1\sigma$  level. This initial sample was further restricted to the objects with an observed flux in the  $\text{H}\beta$  emission line larger than  $10^{-14} \text{ erg s}^{-1} \text{ cm}^{-2}$  and for which accurate abundances could be derived. They have also excluded all galaxies with both  $[\text{O III}]\lambda 4959/\text{H}\beta < 0.7$  and  $[\text{O II}]\lambda 3727/\text{H}\beta > 1.0$ . Applying all these selection criteria, they obtain a sample of  $\sim 310$  SDSS objects. Data for these sample objects include the emission line intensities of  $[\text{O III}]\lambda 4959, 5007 \text{ \AA}$  and  $[\text{N II}]\lambda 6584$  relative to  $\text{H}\beta$  and the EW of  $\text{H}\beta$ . They also include the intensity of the  $[\text{O II}]\lambda\lambda 3727, 3729 \text{ \AA}$  emission line for the lowest redshift objects.

The very young stellar population during the first Ma after each burst produces a high ionization, so the  $[\text{O III}]/\text{H}\beta$  ratio is high, then it decreases raising again at 4 Ma due to the presence of Wolf–Rayet stars that produces a harder continuum (García-Vargas et al. 1995a, 1998). After 5 Ma, the burst evolves to lower values of  $\log[\text{O III}]/\text{H}\beta$ . Diagonal lines in this plot correspond to nearly constant ionization parameter and are swept along by the different successive bursts of a given age. High-excitation objects, with high  $\log[\text{O III}]/\text{H}\beta$  and low  $\log[\text{O II}]/\text{H}\beta$  ratios, have low metallicities and they are not reproduced by our model, which fits better the high-metallicity sample, in the middle to right-hand side of the panel.

It can be better seen in Fig. 9, which shows the relation between the excitation parameter,  $\log([\text{O III}]/\text{H}\beta)$ , and the metallicity indicator  $\log([\text{N II}]/\text{H}\alpha)$  which gives information about the younger populations plus the star formation rate (Kennicutt, Tamblyn & Congdon 1994). At the beginning of the evolution, as we saw in previous sections, the star formation rate is high, and the  $\text{H}\alpha$  emission of our model is strong. As the galaxy evolves, the  $\text{H}\alpha$  emission decreases while the  $[\text{N II}]$  emission increases due to the growth of metallicity.

Our models reproduce the general trend shown by data but cannot reproduce the lower metallicity (low  $[\text{N II}]/\text{H}\alpha$  ratio) objects to the left-hand side of the graph. This is due to the fact that the efficiency of the first burst, 33.1 per cent, produces a metallicity which is already too high. A lower efficiency is therefore required to reproduce the observations of the less metallic objects.

**Table 1.** Evolution of continuum and total broad-band colours for different bursts along the time after each stellar burst occurs. Only the last burst evolution is shown. The whole table is available in electronic format.

NB	$\log(t/a)$	$(U - B)_c$	$(B - V)_c$	$(V - R)_c$	$(V - I)_c$	$(U - B)$	$(B - V)$	$(V - R)$	$(V - I)$	$U$ (per cent)	$B$ (per cent)	$V$ (per cent)	$R$ (per cent)	$I$ (per cent)
11	5.75	-1.205	0.019	0.271	0.480	-1.292	0.748	0.109	0.064	21.254	14.681	57.230	50.400	37.264
11	5.80	-1.202	0.015	0.267	0.474	-1.300	0.694	0.147	0.102	21.845	14.497	54.820	49.812	36.728
11	5.85	-1.203	0.014	0.267	0.472	-1.301	0.706	0.142	-0.065	21.900	14.506	55.610	50.230	42.959
11	5.90	-1.203	0.012	0.264	0.468	-1.311	0.678	0.164	0.117	22.634	14.424	54.460	50.115	37.121
11	5.95	-1.200	0.008	0.260	0.461	-1.345	0.611	0.222	0.177	25.040	14.260	51.674	50.000	37.274
11	6.00	-1.198	0.004	0.255	0.453	-1.378	0.555	0.269	0.225	27.207	13.997	49.152	49.839	37.295
11	6.05	-1.197	0.001	0.252	0.448	-1.383	0.535	0.281	0.236	27.391	13.889	48.246	49.628	37.110
11	6.10	-1.196	-0.002	0.248	0.441	-1.397	0.500	0.307	0.260	28.277	13.716	46.603	49.456	36.942
11	6.15	-1.191	-0.009	0.238	0.426	-1.435	0.407	0.374	0.327	30.679	13.226	41.893	48.686	36.373
11	6.20	-1.189	-0.015	0.232	0.414	-1.457	0.355	0.412	0.363	31.957	12.892	39.095	48.422	36.106
11	6.25	-1.185	-0.021	0.224	0.401	-1.477	0.300	0.452	0.399	33.171	12.523	36.012	48.132	35.917
11	6.30	-1.172	-0.035	0.202	0.367	-1.517	0.136	0.554	0.504	35.548	11.422	25.592	46.160	34.394
11	6.35	-1.160	-0.047	0.182	0.335	-1.515	0.027	0.601	0.551	35.367	10.370	17.718	44.104	32.609
11	6.40	-1.138	-0.067	0.148	0.278	-1.475	-0.068	0.608	0.551	33.098	8.712	9.986	41.101	30.006
11	6.45	-1.113	-0.083	0.116	0.226	-1.403	-0.107	0.543	0.483	29.051	7.251	6.539	36.974	26.347
11	6.50	-1.073	-0.107	0.061	0.128	-1.274	-0.152	0.407	0.336	20.862	4.735	2.161	28.889	19.217
11	6.60	-1.020	-0.076	0.084	0.182	-1.079	0.316	0.000	0.041	12.736	4.400	32.054	24.293	16.869
11	6.70	-0.878	-0.006	0.119	0.277	-0.976	0.024	0.196	0.272	10.700	2.135	6.592	13.066	6.218
11	6.80	-0.484	0.174	0.206	0.446	-0.497	0.140	0.238	0.447	1.707	0.518	0.000	2.901	0.239
11	6.90	-0.553	0.244	0.291	0.617	-0.553	0.212	0.304	0.617	0.295	0.265	0.000	1.341	0.018
11	7.00	-0.630	0.219	0.331	0.723	-0.628	0.190	0.339	0.723	0.029	0.146	0.000	0.706	0.001
11	7.10	-0.567	0.210	0.152	0.698	-0.567	0.182	0.314	0.698	0.000	0.059	0.00	0.00	0.00

### 3.4 Combined continuum and emission line colours

Once the continuum SEDs and the different emission line fluxes are computed, we can calculate the contribution of these emission lines to the different broad-band filters and then synthesize the colours of our model galaxies. These are the colours which are readily observable through integrated photometry.

We have done so taking into account only the strongest emission lines that contribute to the colour in each broad-band spectral interval at redshift zero. These are:  $[\text{O II}] \lambda\lambda 3727, 3729 \text{ \AA}$  in  $U$ ,  $\text{H}\beta \lambda 4861 \text{ \AA}$  in  $B$ ,  $[\text{O III}] \lambda\lambda 4959, 5007 \text{ \AA}$  in  $V$ ,  $\text{H}\alpha \lambda 6563 \text{ \AA}$  in  $R$  and  $[\text{S III}] \lambda\lambda 9069, 9532 \text{ \AA}$  in  $I$ .

The continuum colours and the colours including the emission line contribution at redshift zero are given in columns 3–10 of Table 1 for each of the models characterized by their burst number and age (columns 1 and 2). Columns 11–15 of the same table give the contribution, in percentage, by the emission lines to the different continuum fluxes.

The necessary information to calculate these contributions for any other redshifts in the nearby universe ( $z \lesssim 0.1$ ) is given in Table 2 which lists for each of the models characterized by their burst number and age (columns 1 and 2), the continuum fluxes in each of the  $U, B, V, R$  and  $I$  (columns 3–7) and the fluxes in the  $[\text{O II}]$ ,  $\text{H}\beta$ ,  $[\text{O III}]$ ,  $\text{H}\alpha$  and  $[\text{S III}]$  lines (columns 8–12).

Fig. 7 shows, with dotted lines, the new computed colours including the contribution by the different emission lines. As it can be seen the colours do not change by a large amount in the case of  $U - B$  or  $V - R$ . However, the effect in the  $B - V$  and  $V - I$  colours is rather dramatic. Fig. 10 shows the  $B - V$  versus  $V - I$  colour–colour diagram for model A2. Light blue circles show the continuum colours (solid lines in Fig. 7) while black solid ones show the colours computed including the contribution by the stronger emission lines given in Table 1. The inclusion of the contribution by the emission lines to the continuum colours shifts the position of the model points almost

perpendicularly to the originally computed ones. The location of blue points is mainly determined, even at zero redshift, by the contribution of strong  $[\text{O III}] \lambda\lambda 4959, 5007$  emission lines to the  $V$  band. In the same diagram we show the data by Cairós et al. (2001a,b) on BCG as red squares with error bars. These correspond to readily observed colours therefore including both continuum and line emission. No reddening correction has been applied. It can be seen that some of the data are impossible to reproduce by the models which do not take into account the contribution by emission lines, even if some amount of reddening is invoked (the arrow in the diagram shows the correction corresponding to 1-mg visual extinction), while a certain amount of reddening would bring most of the data in agreement with the models. On the other hand the data by Cairós et al. (2002) of resolved locations in Mrk 370, shown in the figure as green triangles, correspond to data that have been corrected for the contribution by emission lines and therefore correspond to pure continuum colours. In these cases, the agreement with the models is excellent.

## 4 DISCUSSION

The evolution of  $\text{H II}$  galaxies must be considered by looking simultaneously at both continuum and emission line properties, the first one providing information on a long time-scale evolution, of the order of Ga, and the second one being related to the evolution in a much shorter time-scale, of the order of Ma.

Dottori (1981) suggested the use of the EW of  $\text{H}\beta$ ,  $\text{EW}(\text{H}\beta)$ , as an age estimator for  $\text{H II}$  regions, and applied this method to rank the ages of  $\text{H II}$  regions in the Magellanic Clouds. If an SSP is considered, the  $\text{H}\beta$  emission is very high at the beginning of the burst, while the continuum at  $\text{H}\beta$ , dominated by the most massive and luminous stars, is low hence producing a large value of  $\text{EW}(\text{H}\beta)$ . As the burst evolves, the  $\text{H}\beta$  luminosity decreases as does the number of ionizing photons, and the contribution to the continuum increases

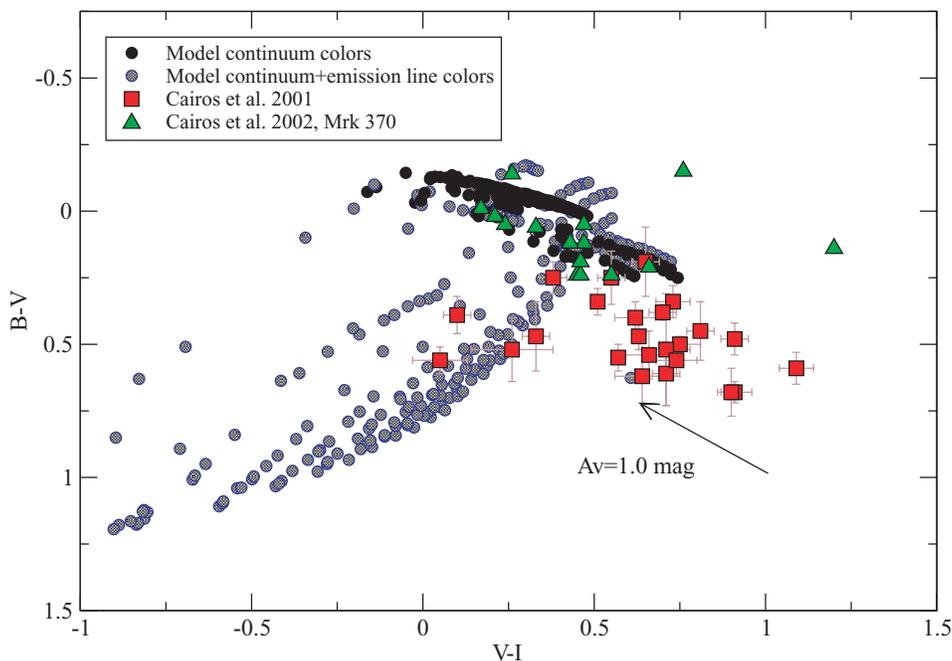
**Table 2.** Evolution of broad-band and the strongest emission lines luminosities along the time after each stellar burst occurs. Only the last burst evolution is shown. The whole table is available in electronic format.

NB	$\log(t/a)$	$L_U$	$L_B$	$L_V$	$L_R$	$L_I$	$L([\text{O II}])$	$L(\text{H}\beta)$	$L([\text{O III}])$	$L(\text{H}\alpha)$	$L([\text{S III}])$
$10^{40} \text{ erg s}^{-1}$											
11	5.75	1.559E+01	1.423E+01	7.080E+00	1.123E+01	7.442E+00	4.252E+00	2.474E+00	9.574E+00	1.1533E+01	4.466E+00
11	5.80	1.569E+01	1.435E+01	7.126E+00	1.126E+01	7.442E+00	4.431E+00	2.458E+00	8.812E+00	1.1296E+01	4.364E+00
11	5.85	1.582E+01	1.447E+01	7.172E+00	1.134E+01	7.483E+00	4.483E+00	2.480E+00	9.080E+00	1.1560E+01	4.459E+00
11	5.90	1.595E+01	1.460E+01	7.225E+00	1.139E+01	7.510E+00	4.716E+00	2.487E+00	8.731E+00	1.1560E+01	4.480E+00
11	5.95	1.612E+01	1.478E+01	7.286E+00	1.144E+01	7.524E+00	5.439E+00	2.483E+00	7.872E+00	1.1560E+01	4.518E+00
11	6.00	1.631E+01	1.500E+01	7.367E+00	1.151E+01	7.552E+00	6.160E+00	2.466E+00	7.196E+00	1.1560E+01	4.538E+00
11	6.05	1.654E+01	1.519E+01	7.448E+00	1.161E+01	7.601E+00	6.303E+00	2.476E+00	7.016E+00	1.1560E+01	4.532E+00
11	6.10	1.680E+01	1.545E+01	7.545E+00	1.172E+01	7.650E+00	6.692E+00	2.481E+00	6.654E+00	1.1586E+01	4.528E+00
11	6.15	1.714E+01	1.584E+01	7.685E+00	1.184E+01	7.685E+00	7.666E+00	2.439E+00	5.598E+00	1.1349E+01	4.439E+00
11	6.20	1.751E+01	1.622E+01	7.835E+00	1.199E+01	7.756E+00	8.309E+00	2.425E+00	5.082E+00	1.1375E+01	4.429E+00
11	6.25	1.792E+01	1.666E+01	8.003E+00	1.216E+01	7.821E+00	8.986E+00	2.410E+00	4.551E+00	1.1401E+01	4.429E+00
11	6.30	1.856E+01	1.746E+01	8.281E+00	1.234E+01	7.850E+00	1.034E+01	2.275E+00	2.878E+00	1.0689E+01	4.158E+00
11	6.35	1.927E+01	1.833E+01	8.599E+00	1.257E+01	7.908E+00	1.065E+01	2.143E+00	1.871E+00	1.0021E+01	3.866E+00
11	6.40	2.050E+01	1.990E+01	9.172E+00	1.299E+01	8.003E+00	1.024E+01	1.919E+00	1.028E+00	9.1614E+00	3.467E+00
11	6.45	2.172E+01	2.158E+01	9.810E+00	1.349E+01	8.152E+00	8.986E+00	1.704E+00	6.936E-01	7.9977E+00	2.946E+00
11	6.50	2.478E+01	2.554E+01	1.136E+01	1.485E+01	8.631E+00	6.600E+00	1.282E+00	2.535E-01	6.0948E+00	2.074E+00
11	6.60	1.929E+01	2.088E+01	9.543E+00	1.273E+01	7.615E+00	2.165E+00	7.670E-01	3.724E+00	3.4910E+00	1.375E+00
11	6.70	1.260E+01	1.556E+01	7.566E+00	1.043E+01	6.596E+00	1.526E+00	3.431E-01	5.396E-01	1.5847E+00	4.419E-01
11	6.80	1.012E+01	1.795E+01	1.023E+01	1.528E+01	1.041E+01	1.776E-01	9.445E-02	0.000E+00	4.6128E-01	2.525E-02
11	6.90	7.074E+00	1.177E+01	7.146E+00	1.154E+01	8.520E+00	2.121E-02	3.171E-02	0.000E+00	1.5847E-01	1.615E-03
11	7.00	5.045E+00	7.821E+00	4.648E+00	7.799E+00	6.110E+00	1.491E-03	1.159E-02	0.000E+00	5.6100E-02	8.127E-05
11	7.10	4.390E+00	7.205E+00	4.247E+00	7.009E+00	5.456E+00	6.406E-08	4.361E-03	0.000E+00	2.0891E-05	0.000E+00

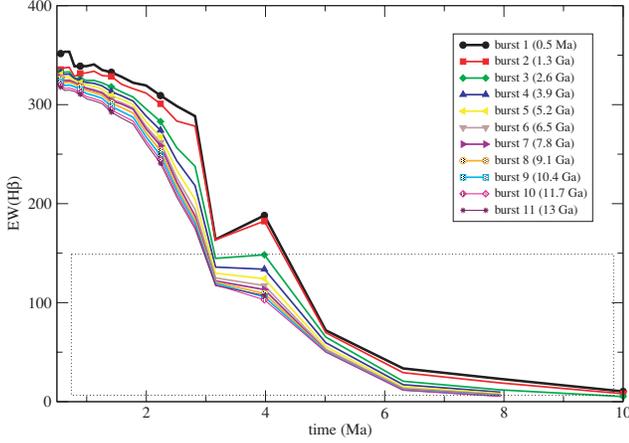
thus lowering the value of  $\text{EW}(\text{H}\beta)$ . This case corresponds to the thick (black) line in Fig. 11.

The evolution of the EW in our model is shown in Fig. 11. It is seen that the first burst, which corresponds to an SSP, has an initial EW slightly greater than the successive bursts, which decreases with time reaching very low values ( $<40 \text{ \AA}$ ) 6 Ma after the beginning. When a new burst takes place, new massive ionizing stars form and the  $\text{EW}(\text{H}\beta)$  goes up again, although not as much

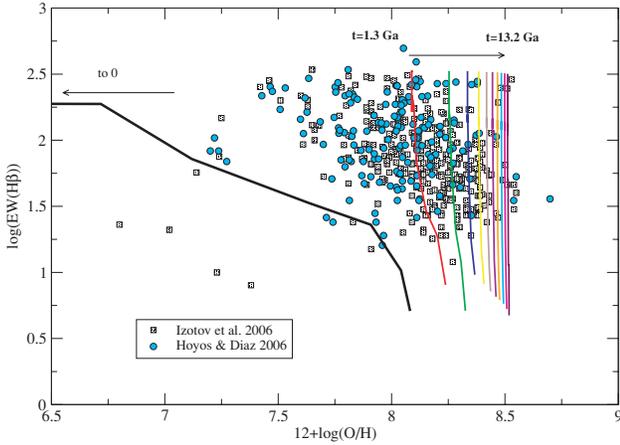
as in the previous one due to the decreasing gas mass involved in the burst, increased metallicity and the accumulated contribution from the continua from the previous bursts. At any rate, even taking into account this contribution, the  $\text{EW}(\text{H}\beta)$  remains a good age indicator for the age of the current burst, inside 10 Ma. On the other hand it is not possible to detect the presence of the underlying stellar populations for a given galaxy solely on the basis of this parameter.



**Figure 10.**  $B - V$  versus  $V - I$  colour-colour diagram for model A2. Light blue circles show the continuum colours (solid lines in Fig. 7) while black solid ones show the colours computed including the contribution by the stronger emission lines. The data by Cairós et al. (2001a) on BCG and Cairós et al. (2002) in Mrk 370 are included as red squares and green triangles, respectively.



**Figure 11.** Time evolution of the  $H\beta$  EW of model A2. The thick line corresponds to the first starburst of our model, an SSP with very low metallicity. Thin lines represent the successive bursts with same colours as in Fig. 5.



**Figure 12.**  $EW(H\beta)$  as a function of the metallicity  $12 + \log(O/H)$  for the model A2. Colours have the same meaning than in Fig. 7. The first burst (solid black line) does not appear in the graph because its abundance is still the primordial one,  $12 + \log(O/H) \ll 7$ .

The distribution of the  $EW(H\beta)$  in  $H\text{ II}$  galaxies shows that most of them have values lower than  $150 \text{ \AA}$  (Terlevich et al. 1991; Hoyos & Díaz 2006) which, in our models, corresponds to ages greater than 3–4 Ma. Terlevich et al. (2004), from the application of inversion methods, have shown that, globally, this distribution is inconsistent with what is expected from a single burst scenario and resembles more the distribution obtained for a succession of short bursts separated by quiescent periods with little or no star formation.

These results are not that strong when samples showing a restricted metallicity range are analysed. However, as we have seen before, metallicity increases with time in a way which constrains the SFH which is best reproduced by our A2 model. Fig. 12 shows the evolution of the  $EW(H\beta)$  with oxygen abundance. During the duration of the first burst the  $EW(H\beta)$  decreases while the oxygen abundance increases from 0 to  $12 + \log(O/H) \sim 8$ . The successive bursts start with this higher abundance and each of them evolves vertically in a 10 Ma time-scale with the  $EW(H\beta)$  decreasing rapidly at almost constant oxygen abundance. This occurs because the oxygen is produced by the most massive stars in a very short time and therefore its abundance changes very little during the next 10 Ma

after each burst (see Fig. 3). It is clear that our model is able to reproduce the most metallic galaxies in the samples taken from Hoyos & Díaz (2006) and Izotov et al. (2006) where this high abundance is explained as the consequence of the gas being processed by one or more previous generations of stars. An alternative scenario to produce such high oxygen abundances would be the occurrence of a very intense initial star formation burst, with a SFR of the order of  $100 M_{\odot} \text{ Ma}^{-1}$ , out of the range observed in local  $H\text{ II}$  galaxies (see Figs 3 and 1). On the other hand, galaxies  $12 + \log(O/H) \leq 8$  are not reproduced by our model. In order to fit these data, a model with a star formation efficiency lower than assumed, i.e.  $<33$  per cent, should be used.

The most informative data to uncover the presence of underlying populations in  $H\text{ II}$  galaxies consist of the combination of a line emission parameter, which characterizes the properties of the current burst of star formation, and a continuum colour which represents better the SFH in a longer time-scale. Fig. 13, left-hand panel, shows the  $EW$  of  $H\beta$  versus the  $U - V$  colour along the evolution of the galaxy for the successive stellar bursts. When a given burst occurs the  $EW(H\beta)$  is high and decreases as the stellar population ages. We have overplotted the results for the SSPs from the model STARBURST99 (Leitherer et al. 1999, hereafter SB99) with two different metallicities as labelled. As expected, our results agree better with the higher metallicity SB99 model. The black line in the left-hand panel, which represents a metal-poor SSP, is too blue compared with the data for a given  $EW(H\beta)$ . In order to decrease  $EW(H\beta)$  and move the model colour to the red, a more metal-rich SSP was selected (dotted line at the left-hand panel), but even such unrealistic high abundance does not reproduce the observations, as we have shown in Fig. 3. Therefore, the observed trend cannot be explained as an age effect since  $EW(H\beta)$  for low-metallicity SSP does not reach values lower than  $100 \text{ \AA}$  and does not reproduce the colours, neither as a metallicity effect because such high abundances are not observed in  $H\text{ II}$  galaxies. It is therefore necessary to include both effects simultaneously, as we have done, to see how the effect of an underlying older population contributing to the colour of the continuum makes it redder. From the observational point of view,  $U - V$  colours for  $H\text{ II}$  galaxies are scarce, therefore we have compared our results with those from Hoyos & Díaz (2006) that include galaxies taken from Terlevich et al. (1991) and Salzer et al. (1995) providing the EWs of both the  $[O\text{ II}]\lambda 3727$  and  $[O\text{ III}]\lambda 5007$  lines. We have then computed pseudo-colours from the intensities of the adjacent continua of  $[O\text{ II}]\lambda 3727$  and  $[O\text{ III}]\lambda 5007$  lines as

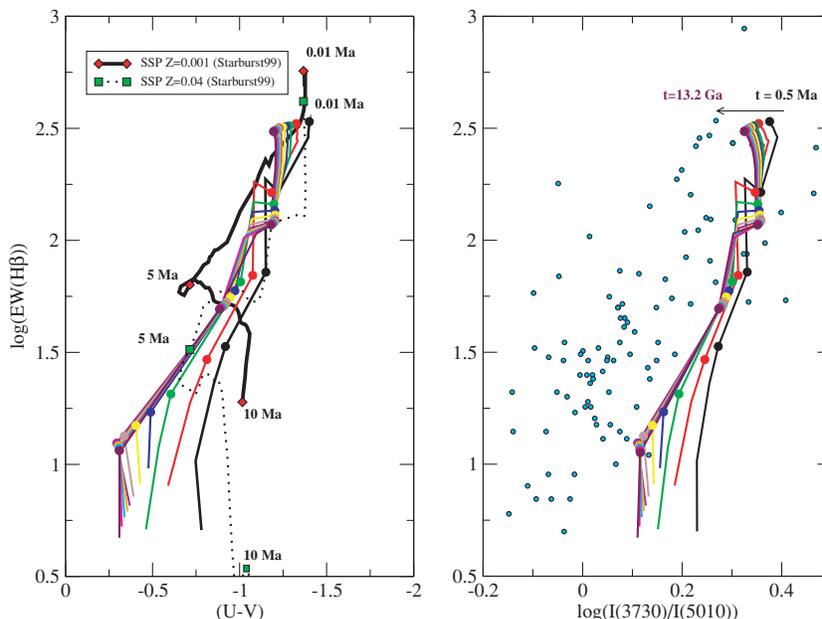
$$EW_{[O\text{ II}]\lambda 3727} (\text{\AA}) = \frac{[O\text{ II}]\lambda 3727 (\text{erg s}^{-1})}{I_{\text{cont}}(3730) (\text{erg s}^{-1} \text{\AA}^{-1})} \quad (12)$$

and

$$EW_{[O\text{ III}]\lambda 5007} (\text{\AA}) = \frac{[O\text{ III}]\lambda 5007 (\text{erg s}^{-1})}{I_{\text{cont}}(5010) (\text{erg s}^{-1} \text{\AA}^{-1})}, \quad (13)$$

$$\log \left( \frac{I_{\text{cont}}(3730)}{I_{\text{cont}}(5010)} \right) = \log \left( \frac{[O\text{ II}]\lambda 3727 EW_{[O\text{ III}]\lambda 5007}}{[O\text{ III}]\lambda 5007 EW_{[O\text{ II}]\lambda 3727}} \right). \quad (14)$$

The right-hand panel of Fig. 13 shows the  $EW$  of  $H\beta$  as a function of the pseudo-colour defined above for model A2 together with the observational data. It should be noted that no correction for extinction associated with the continuum light has been made. This correction amounts to about 0.15 dex for a standard reddening law and therefore an SSP would always be unable to reproduce the observed colours. Yet our model A2 produce UV continuum colours which are too blue as compared with the bulk of the observations which indicates that our assumed degree of attenuation is too low.



**Figure 13.** Left-hand panel: The EW of  $H\beta$  as a function of the continuum colour for model A2. The results for the SSPs from the model STARBURST99 (SB99) with two different metallicities as labelled are overplotted. Colours have the same meaning as in Fig. 7. Right-hand panel: The EW of  $H\beta$  as a function of the pseudo-colour defined by equations (12)–(14) for model A2. The data are from Terlevich et al. (1991) and Salzer et al. (1995). In both panels the large dots mark ages separated 2 Ma.

## 5 SUMMARY AND CONCLUSIONS

We have explored the viability of a kind of a theoretical model in order to understand how the star formation takes place in  $H\text{ II}$  galaxies. Our work involves the combination of three different tools: a chemical evolution code, an evolutionary synthesis code and a photoionization code, in a self-consistent way, i.e. taking the same assumptions about stellar evolution and nucleosynthesis, and takes into account the resulting metallicity in every time-step. The chemical evolution code provides the SFH of the galaxies as well as the time evolution of the abundances in their ISM, which can be confronted with observations. The evolutionary synthesis code provides the spectrophotometric evolution of the integrated stellar population. Finally, the photoionization code uses the properties of the ionizing stellar population to calculate the emission line spectra of the ionized gas.

Each galaxy is modelled assuming an initial amount of unprocessed gas of  $10^8 M_{\odot}$  in a 1 kpc diameter. The evolution is computed along a total duration of 13.2 Ga during which 11 successive starbursts, separated by 1.3 Ga, take place. Different types of models have been computed with different starbursting properties: equal and attenuated bursts, and different values of the initial star formation efficiency. The only model which has proved to be able to fit the observational data is model A2, which consists of attenuated bursts with an initial star formation efficiency of 33.1 per cent. This type of model reproduces the star formation rate estimates of local  $H\text{ II}$  galaxies and the oxygen abundances of the average metallicity objects although fails to account for the most metal deficient ones which would require models with lower star formation efficiencies than assumed.

We have computed the time evolution of the continuum colours with and without the inclusion of the emission lines. It is shown that both nebular continuum and line emission must be taken into account in the photometric studies of the underlying stellar populations of

$H\text{ II}$  galaxies. The effect of the emission lines are more pronounced in the  $B - V$  and  $V - I$  colours.

The combination of parameters which characterize the current star formation on a time-scale of Ma, such as the EW of  $H\beta$ , and the SFH over a time-scale of Ga, such as broad-band continuum colours, is found to provide an effective means to uncover the presence of underlying stellar populations. The comparison of models and observations show that in most  $H\text{ II}$  galaxies SSP are unable to reproduce the relatively red colours shown by data with the observed  $H\beta$  EW values requiring the contribution of previous stellar generations. Our model, however, produces  $U - V$  colours that are too blue when compared with observations, therefore implying that the successive bursts that take place in  $H\text{ II}$  galaxies should be even more attenuated than has been assumed in our work.

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## SUPPLEMENTARY MATERIAL

The following supplementary material is available for this article:

**Table 1.** Evolution of continuum and total broad-band colours for different bursts along the time after each stellar burst occurs.

**Table 2.** Evolution of broad-band and the strongest emission lines luminosities along the time after each stellar burst occurs.

This material is available as part of the online article from: <http://www.blackwell-synergy.com/doi/abs/10.1111/j.1365-2966.2007.12875.x>  
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