

Dark Energy Survey Year 1 Results: Cross-correlation between Dark Energy Survey Y1 galaxy weak lensing and South Pole Telescope + *Planck* CMB weak lensing

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We cross-correlate galaxy weak lensing measurements from the Dark Energy Survey (DES) year-one data with a cosmic microwave background (CMB) weak lensing map derived from South Pole Telescope (SPT) and *Planck* data, with an effective overlapping area of 1289 deg². With the combined measurements from four source galaxy redshift bins, we obtain a detection significance of 5.8 σ . We fit the amplitude of the correlation functions while fixing the cosmological parameters to a fiducial Λ CDM model, finding $A = 0.99 \pm 0.17$. We additionally use the correlation function measurements to constrain shear calibration bias, obtaining constraints that are consistent with previous DES analyses. Finally, when performing a cosmological analysis under the Λ CDM model, we obtain the marginalized constraints of $\Omega_m = 0.261_{-0.051}^{+0.070}$ and $S_8 \equiv \sigma_8 \sqrt{\Omega_m/0.3} = 0.660_{-0.100}^{+0.085}$. These measurements are used in a companion work that presents cosmological constraints from the joint analysis of two-point functions among galaxies, galaxy shears, and CMB lensing using DES, SPT, and *Planck* data.

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I. INTRODUCTION

As a photon from a distant source travels through the Universe, its path is perturbed by the gravitational potential of large-scale structure, an effect known as gravitational lensing (for a review see e.g., [1]). The observed amplitude of the perturbations to the photon's trajectory depends on both the matter distribution and geometry of the Universe, making gravitational lensing a powerful cosmological probe. Furthermore, because these perturbations are induced by gravitational effects, they are sensitive to all forms of matter, including dark matter, which is difficult to probe by other means. The use of gravitational lensing to constrain cosmology has developed rapidly over the past decade [2–10] due to improvements in instrumentation and modeling, and it increases in the cosmological volumes probed by surveys [11,12].

In this study, we use two sources of photons to measure the effect of gravitational lensing: distant galaxies and the cosmic microwave background (CMB). Gravitational lensing caused by the large-scale distribution of matter distorts the apparent shapes of distant galaxies; similarly, gravitational lensing distorts the observed pattern of temperature fluctuations on the CMB last scattering surface. These distortions are expected to be correlated over the same patch of sky since the CMB photons pass through some of the same intervening gravitational potentials as the photons from distant galaxies. The two-point correlation between the galaxy lensing and CMB lensing fields can therefore be used as a cosmological probe.

Several features of the cross-correlation between galaxy lensing and CMB lensing make it an appealing cosmological observable. First, unlike two-point correlations

between galaxies and lensing, the lensing-lensing correlation considered here has the advantage that it is not sensitive to difficult-to-model effects such as galaxy bias [13]. Second, since it is a cross-correlation between two independently measured lensing fields from datasets of completely different natures, it is expected to be relatively robust to observational systematics. For instance, systematics associated with galaxy shape measurement, such as errors in the estimate of the point spread function, will have no impact on the inference of CMB lensing. Third, the use of the CMB lensing field provides sensitivity to the distance to the last scattering surface; the large distance to the last scattering surface in turn provides a long lever arm for constraining cosmology.

Measurement of the two-point correlation between galaxy lensing and CMB lensing was first reported by [14] using CMB lensing measurements from the Atacama Cosmology Telescope [15] and galaxy lensing measurements from the Canada-France-Hawaii Telescope Stripe-82 Survey [16]. Several subsequent measurements were made by [17] (*Planck* CMB lensing + CFHTLenS galaxy lensing), [18] (*Planck* and SPT CMB lensing + DES-SV galaxy lensing), [19] (*Planck* CMB lensing + CHTLenS and RCSLenS galaxy lensing), and [20] (*Planck* CMB lensing + KiDS-450 galaxy lensing).

Here we measure the correlation between CMB lensing and galaxy lensing using CMB data from the South Pole Telescope (SPT) and *Planck*, and galaxy lensing data from year-one (Y1) observations of the Dark Energy Survey (DES; [21]). We perform a number of robustness checks on the measurements and covariance estimates to show that there is no evidence for significant systematic biases in the measurements over the range of angular scales that we include in the model fits.

The measurements presented here represent the highest signal-to-noise constraints on the cross-correlation between galaxy lensing and CMB lensing to date. We use the measured correlation functions to place constraints on cosmological parameters (in particular Ω_m and $S_8 = \sigma_8 \sqrt{\Omega_m/0.3}$). The cosmological constraints obtained here are complementary to those from DES-Y1 galaxy clustering and weak lensing [12], which are sensitive to somewhat lower redshifts.

This work is part of a series of four papers that use cross-correlations between DES data and CMB lensing measurements to constrain cosmology:

- (i) Measurement of correlation between galaxy lensing and CMB lensing (this paper);
- (ii) Measurement of correlation between galaxies and CMB lensing [22];
- (iii) Methodology for analyzing joint measurements of correlations between DES data and CMB lensing [23];
- (iv) Results of joint analysis of correlations between DES data and CMB lensing [24].

The main goal of this work is to present the measurement of the correlation between galaxy lensing and CMB lensing, and to subject this measurement to robustness tests. Consequently, we keep discussion of the cosmological modeling brief and refer the readers to [23] for a more in-depth discussion of the cosmological modeling used in these papers.

This work is organized as follows. In Sec. II we present the theoretical background of the analysis and the required formalism used throughout the analysis. We describe the data products used in Sec. III and the methodology used to make the measurements in Sec. IV. The results are presented in Sec. V, while the cosmological parameter fits are shown in Sec. VI. Finally, we present our conclusions in Sec. VII.

II. THEORY

We are interested in the cross-correlation between CMB lensing and galaxy lensing. CMB lensing is typically measured in terms of the spin-0 lensing convergence, κ , which is proportional to a (weighted) integral along the line of sight of the matter density [25]. Galaxy lensing, on the other hand, is most easily measured via the spin-2 shear field, γ , by measuring shapes of many galaxies. The γ and κ signals are related, and one could in principle convert from γ to κ (e.g., [26]). However, the conversion process is lossy, and not necessary for our purposes since we can directly correlate κ and γ . The galaxy shear signal is estimated from the coherent distortion of the shapes of galaxies. In this analysis, we measure the correlation of the CMB lensing convergence, κ_{CMB} , with the *tangential* component of the galaxy shear, γ_t (i.e., the component orthogonal to the line connecting the two points being correlated). The advantages of using γ_t are that it can be computed directly from the observed shapes of galaxies. This approach was recently used by [19], who found it to yield higher signal to noise than alternative approaches; the same approach was also taken by [27].

To quantify the correlation between CMB lensing and galaxy lensing, we use the angular two-point function, $w^{\gamma_t \kappa_{\text{CMB}}}(\theta)$. To model this correlation, we begin by calculating the theoretical cross-power spectrum between the CMB lensing convergence and the galaxy lensing convergence, κ_{CMB} and κ_s , which we denote with $C^{\kappa_s \kappa_{\text{CMB}}}(\ell)$. In harmonic space and using the Limber approximation [28,29], we have

$$C^{\kappa_s \kappa_{\text{CMB}}}(\ell) = \int_0^{\chi_*} \frac{d\chi}{\chi^2} q_{\kappa_s^i}(\chi) q_{\kappa_{\text{CMB}}}(\chi) P_{\text{NL}} \left(k = \frac{\ell + \frac{1}{2}}{\chi}, z(\chi) \right), \quad (1)$$

$$q_{\kappa_s^i}(\chi) = \frac{3\Omega_m H_0^2}{2c^2} \frac{\chi}{a(\chi)} \int_{\chi}^{\chi_h} d\chi' \frac{n_s^i(z(\chi'))}{\bar{n}_s^i} \frac{dz}{d\chi'} \frac{\chi' - \chi}{\chi'}, \quad (2)$$

$$q_{\kappa_{\text{CMB}}}(\chi) = \frac{3\Omega_{\text{m}}H_0^2}{2c^2} \frac{\chi}{a(\chi)} \frac{\chi_* - \chi}{\chi_*}. \quad (3)$$

Here, χ is the comoving distance, χ_* is the comoving distance to the last scattering surface, $a(\chi)$ is the cosmological scale factor at distance χ , $n_s^i(z)$ is the redshift distribution of the source galaxies in the i th redshift bin, $\bar{n}_s^i = \int dz n_s^i(z)$ is the angular number density in this redshift bin, and $P_{\text{NL}}(k, z)$ is the nonlinear matter power spectrum at wave number k and redshift z . We calculate P_{NL} using the Boltzmann code CAMB¹ [30,31] with the Halofit extension to nonlinear scales [32,33] and the [34] neutrino extension.

The harmonic-space cross spectrum between the CMB and galaxy convergences can be transformed to a position-space correlation function by taking the Hankel transform

$$w^{\gamma_i \kappa_{\text{CMB}}}(\theta) = \int_0^\infty \frac{\ell d\ell}{2\pi} C^{\kappa_i \kappa_{\text{CMB}}}(\ell) J_2(\ell\theta) F(\ell), \quad (4)$$

where J_2 is the second order Bessel function of the first kind and $F(\ell)$ describes filtering that is applied to the CMB lensing map (see Sec. III). We set

$$F(\ell) = \begin{cases} \exp(-\ell(\ell+1)/\ell_{\text{beam}}^2), & \text{for } 30 < \ell < 3000, \\ 0, & \text{otherwise,} \end{cases} \quad (5)$$

with $\ell_{\text{beam}} \equiv \sqrt{16 \ln 2} / \theta_{\text{FWHM}} \approx 2120$, where $\theta_{\text{FWHM}} = 5.4'$. The filtering is applied to suppress the high- ℓ modes in the noise spectrum. This is to ensure that the covariance matrix does not oscillate rapidly in position space (since we are taking a Hankel transform to convert from harmonic space to position space and the noise spectrum is rising as a function of ℓ). Since we are applying this filtering to both data and theory, the signal to noise is unaffected.

III. DATA

A. Galaxy weak lensing

DES is an optical galaxy survey conducted using the 570 Megapixel DECam instrument [35] mounted on the Blanco Telescope at the Cerro Tololo Inter-American Observatory (CTIO) located in Chile. In this analysis, we use the Y1 data that are based on observation runs between August 2013 and February 2014 [36]. We only use the data in the area overlapping with the SPT footprint²; the overlap area is approximately 1289 deg² between $-60^\circ < \text{Dec} < -40^\circ$, after applying a mask to remove poorly characterized regions.

¹See `camb.info`.

²DES-Y1 data also cover the SDSS Stripe-82 region, though the cosmology analysis focuses on the SPT region.

Two independent shape measurement algorithms—METACALIBRATION and IM3SHAPE—were used to generate two different shear catalogs from DES-Y1 data. These algorithms and the corresponding catalogs are described in detail in [37]. In this analysis, we only consider the METACALIBRATION shear estimates because of the higher signal-to-noise ratio of that catalog.

METACALIBRATION [38,39] is a recently developed technique for measuring galaxy shears that uses the data itself for calibration, rather than relying on external image simulations. The methodology has been demonstrated to yield a multiplicative shear bias below 10^{-3} on simulations with galaxies of realistic complexity [39]. Briefly, METACALIBRATION performs shear calibration by applying artificial shears to the observed galaxy images and measuring the response of the shear estimator. The shear catalog used in this work was based on jointly fitting images in three bands (*riz*).

The full METACALIBRATION catalogue is split into four photometric redshift bins: $0.20 < z < 0.43$, $0.43 < z < 0.63$, $0.63 < z < 0.90$, $0.90 < z < 1.30$ (as shown in Fig. 1), where z is the mean of the estimated redshift probability distribution for each galaxy and the binning is chosen to be consistent with that used in [12]. The redshift distributions, $n_s^i(z)$, for each of the samples were estimated using the BPZ code [40]. Detailed validation of these distributions can be found in [41–43]. We also checked that using an independent $n_s^i(z)$ estimation from the high quality COSMOS2015 photometric redshift catalog [41,44] results in negligible change in the final cosmological constraints.

To avoid implicit experimenter bias, the measurements were blinded while most of the analysis was being performed. The measurements were not compared with theoretical predictions and the axes were removed prior to unblinding. For cosmological parameter estimations, the contours were shifted, and the axes were removed.

B. CMB lensing map

We use the CMB weak lensing map described in [45], which was created from a combination of the SPT and *Planck* CMB temperature data. Details of the κ_{CMB} procedures used to create the map can be found in [45]; we provide a brief overview below.

The lensing map is derived from a minimum-variance combination of SPT 150 GHz and *Planck* 143 GHz temperature maps over the SPT-SZ survey region (20^{h} to 7^{h} in right ascension and from -65° to -40° in declination). By combining SPT and *Planck* maps in this way, the resultant temperature map is sensitive to a greater range of modes on the sky than either experiment alone. Modes in the temperature maps with $\ell > 3000$ are removed to avoid systematic biases due to astrophysical foregrounds such as the thermal Sunyaev-Zel'dovich effect (tSZ) and the cosmic infrared background (CIB) [46], whereas modes with $\ell < 100$ are removed to reduce the effects from low-frequency noise. The quadratic estimator technique [47] is used to

construct a (filtered) estimate of κ_{CMB} . Simulations are used to remove the mean-field bias and to calculate the response function which is used to properly normalize the amplitude of the filtered lensing map.

The output lensing convergence map is filtered further to remove modes with $\ell < 30$ and $\ell > 3000$ and is smoothed with a Gaussian beam with full width at half maximum of $5.4'$. Point sources (dusty-star forming and radio galaxies) with flux density above 6.4 mJy in the 150 GHz band are masked with apertures of $r = 3', 6', 9'$ depending on the brightness of the point source. Additionally, in order to reduce contamination of the κ_{CMB} map by the tSZ signal, we apply a mask to remove clusters detected at signal-to-noise $S/N > 5$ in the SPT CMB maps, and DES REDMAPPER clusters with richness $\lambda > 80$; these clusters are masked with an aperture of $r = 5'$. The effectiveness of this masking at reducing the tSZ contamination was investigated in [23]. Such masking could in principle induce a bias because clusters are associated with regions of high lensing convergence. However, it was shown in [23] that less than 1% of the survey area is lost by applying a mask that removes 437 clusters, and that this leads to a bias of at most 1%.

The effect of the uncertainty on the calibration of the CMB temperature was investigated in [45], and it was found to be at most 0.20σ of the statistical uncertainty when the calibration is conservatively varied by 1% (although it is known to better than 1% as noted in [48]).

IV. METHODS

A. Two-point measurement

Our estimator for the angular correlation function at the angular bin specified by angle θ_α is

$$w^{\gamma\kappa_{\text{CMB}}}(\theta_\alpha) = \frac{\sum_{i=1}^{N_{\text{pix}}} \sum_{j=1}^{N_{\text{gal}}} f_\kappa^i \kappa_{\text{CMB}}^{ij} e_t^{ij} \Theta_\alpha(\hat{\theta}^i - \hat{\theta}^j)}{s(\theta_\alpha) \sum f_\kappa^i}, \quad (6)$$

where the sum in i is over all pixels in the CMB convergence map, the sum in j is over all source galaxies, and $\hat{\theta}$ represents the direction of the κ_{CMB} pixels or source galaxies. e_t^{ij} is the component of the corrected ellipticity oriented orthogonally to the line connecting pixel i and source galaxy j (see e.g., [49]). The κ_{CMB} value in the pixel is κ_{CMB}^i and f_κ^i is the associated pixel masking weight, which takes a value between zero and one (i.e., zero if the pixel is completely masked). The function $\Theta_\alpha(\theta)$ is an indicator function that is equal to unity when the angular separation between $\hat{\theta}_i$ and $\hat{\theta}_j$ is in the angular bin specified by θ_α , and zero otherwise. Finally, $s(\theta_\alpha)$ is the METACALIBRATION response, which can be estimated from the data using the procedure described in [37]. We find that $s(\theta)$ is approximately constant over the angular scales of our interest, but different for each redshift bin.

We evaluate the estimator in Eq. (6) using the TREECORR package.³

We perform the $w^{\gamma\kappa_{\text{CMB}}}(\theta)$ measurements in 10 logarithmic bins over the angular range $2.5' < \theta < 250'$. Later we remove a subrange of these scales in the likelihood analysis, where the scale cuts are determined such that they prevent known sources of systematic error from biasing cosmological constraints (see Sec. IV D).

B. Modeling of systematic effects in galaxy shear measurements

Equation (4) forms the basis for our model of the measured correlation functions. We improve on this basic model by also incorporating prescriptions for systematic errors in the estimated shears and redshift distributions of the galaxies. We describe these models briefly below. For more details, readers should refer to [23,50]. The computation of the model vectors and sampling of parameter space is performed using COSMOSIS [30,32,51–55].

1. Photometric redshift bias

The inference of the redshift distribution, $n_s^i(z)$, for the source galaxy sample is potentially subject to systematic errors. Following [23,50] and related past work [5,56–58], we account for these potential systematic errors in the modeling by introducing a photometric redshift bias parameter which shifts the assumed $n_s^i(z)$ for the source galaxies.⁴ That is, the true redshift distribution for the i th source galaxy bin, $n_{s,\text{unbiased}}^i(z)$, is related to the observed redshift distribution, $n_s^i(z)$, via

$$n_{s,\text{unbiased}}^i(z) = n_s^i(z - \Delta_{z,s}^i), \quad (7)$$

where $\Delta_{z,s}^i$ is the redshift bias parameter, which is varied independently for each source galaxy redshift bin.

Priors on the $\Delta_{z,s}^i$ are listed in Table I. The $\Delta_{z,s}^i$ values for the three lowest redshift bins were obtained by cross correlating the source galaxy sample with REDMAGIC Luminous Red Galaxies (LRGs) [59], which have well characterized redshifts. The $\Delta_{z,s}^i$ value for the highest redshift bin comes from comparing $n_s^i(z)$ derived from BPZ and the COSMOS2015 catalog. The derivation of these priors is described in [41], with two other supporting analyses described in [42,43].

³<https://github.com/rmjarvis/TreeCorr>.

⁴As discussed in [41], the errors in the photo- z distributions are likely to be more complex than a translational shift. We have tested whether the shape of the redshift distribution of the galaxies impact our constraints on cosmological parameters by using a $n(z)$ from a secondary redshift calibration method and found negligible differences in the results.

2. Shear calibration bias

In weak lensing, one estimates galaxy shapes, or ellipticities using a suitably chosen estimator. These estimators are often biased and need to be *calibrated* using either external image simulations (e.g., the IM3SHAPE method) or manipulation of the data itself (e.g., the METACALIBRATION method). The shear calibration bias refers to the residual bias in the shear estimate after the calibration process, or the uncertainty in the calibration process. In particular, we are mainly concerned about the multiplicative bias in the shear estimate, which can arise from failures in the shape measurements, stellar contamination in the galaxy sample, false object detection, and selection bias [61,62].

Following [23,50], we parametrize this systematic error in shear calibration with a single multiplicative factor, $(1 + m^i)$, for each redshift bin i . With this factor, the observed correlation function becomes

$$w_{\text{obs}}^{\gamma_i \kappa_{\text{CMB}}}(\theta) = (1 + m^i) w_{\text{true}}^{\gamma_i \kappa_{\text{CMB}}}(\theta), \quad i \in \{1, 2, 3, 4\}. \quad (8)$$

We let the bias parameter for each redshift bin vary with a Gaussian prior listed in Table I based on [37].

TABLE I. The fiducial parameter values^a and priors for cosmological and nuisance parameters used in this analysis. Square brackets denote a flat prior over the indicated range, while parentheses denote a Gaussian prior of the form $\mathcal{N}(\mu, \sigma)$.

Parameter	Fiducial	Prior
Cosmology		
Ω_m	0.309	[0.1, 0.9]
$A_s/10^{-9}$	2.14	[0.5, 5.0]
n_s	0.967	[0.87, 1.07]
w_0	-1.0	Fixed
Ω_b	0.0486	[0.03, 0.07]
h_0	0.677	[0.55, 0.91]
$\Omega_b h^2$	6.45×10^{-4}	[0.0006, 0.01]
Ω_K	0	Fixed
τ	0.066	Fixed
Shear Calibration Bias		
m^1	0.010	(0.012, 0.023)
m^2	0.014	(0.012, 0.023)
m^3	0.006	(0.012, 0.023)
m^4	0.013	(0.012, 0.023)
Intrinsic Alignment		
A_{IA}	0.44	[-5, 5]
η_{IA}	-0.67	[-5, 5]
z_0	0.62	Fixed
Source Photo- z Error		
$\Delta_{z,s}^1$	-0.004	(-0.001, 0.016)
$\Delta_{z,s}^2$	-0.029	(-0.019, 0.013)
$\Delta_{z,s}^3$	0.006	(0.009, 0.011)
$\Delta_{z,s}^4$	-0.024	(-0.018, 0.022)

^aWe use the *Planck* TT,TE,EE+LENSING+EXT best-fit values from [60] for the cosmological parameters and the marginalized one-dimensional peaks for the DES nuisance parameters from the DES-Y1 joint analysis [12].

3. Intrinsic alignment

In addition to the apparent alignment of the shapes of galaxies as a result of gravitational lensing, galaxy shapes can also be *intrinsically* aligned as a result of their interactions with the tidal field from nearby large-scale structure. The intrinsic alignment (IA) effect will impact the observed correlation functions between galaxy shear and κ_{CMB} [63,64]. The impact of IA can be modeled via

$$C_{\text{obs}}^{\kappa_s \kappa_{\text{CMB}}}(\ell) = C_{\text{true}}^{\kappa_s \kappa_{\text{CMB}}}(\ell) - C^{\kappa_{\text{CMB}}^{\text{I}}}(\ell), \quad (9)$$

where $C^{\kappa_{\text{CMB}}^{\text{I}}}(\ell)$ is calculated in a similar way as Eq. (1), but with replacing the galaxy lensing kernel with

$$W^{\text{I}}(\chi) = A(\chi(z)) \frac{C_{1\rho_{\text{crit}}}\Omega_m n_s^i(z(\chi)) dz}{\mathcal{D}(z) \bar{n}_s^i d\chi}, \quad (10)$$

where $\mathcal{D}(z)$ is the linear growth function. Here we have employed the nonlinear linear alignment model (see [52] for details) and included the redshift evolution of the IA amplitude via

$$A(\chi(z)) = A_{\text{IA}} \left(\frac{1+z}{1+z_0} \right)^{\eta_{\text{IA}}}. \quad (11)$$

We use fixed values $z_0 = 0.62$, $C_{1\rho_{\text{crit}}} = 0.0134$, while letting A_{IA} and η_{IA} vary, as done in [12].

C. Covariance

The covariance matrix of $w^{\gamma_i \kappa_{\text{CMB}}}(\theta)$ is computed analytically, using the halo model to estimate the non-Gaussian contributions. Details of the covariance calculation can also be found in [23,50]. However, we make a small modification in calculating the noise-noise covariance term, which we measure by cross correlating κ_{CMB} noise and rotated galaxy shears. This modification is needed to incorporate the geometry of the mask, which the analytic covariance neglects, and this correction increases the covariance by $\sim 30\%$. We compare the theoretical estimate of the covariance to an estimate of the covariance derived from the data in Sec. VB.

D. Angular scale cuts

There are several effects that may impact the observed correlation functions that we do not attempt to model. As shown in [23], the most significant unmodeled effects for the analysis of $w^{\kappa_{\text{CMB}}\gamma_i}$ are biases in κ_{CMB} due to the tSZ effect, and the impact of baryonic effects on the matter power spectrum. To prevent these effects from introducing systematic errors into our cosmological constraints, we exclude the angular scales from our analysis that are most impacted. Qualitatively, the tSZ bias is small at the smallest scales measured (2.5 arc min), peaks at intermediate scales (around 10 arc min), and then declines again at large scales.

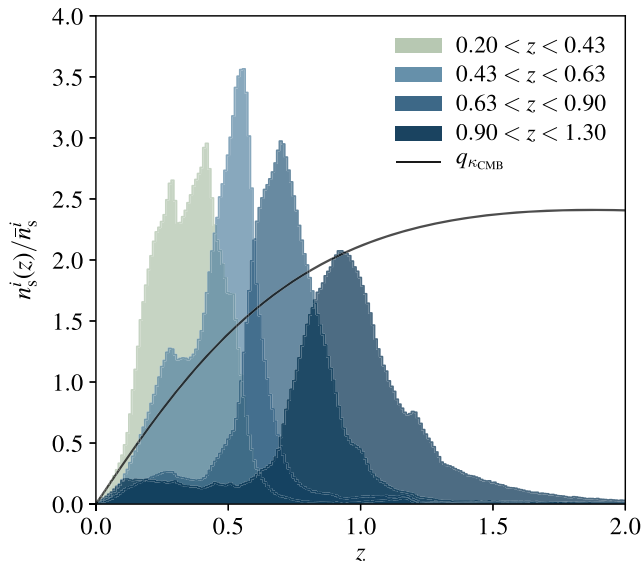


FIG. 1. Redshift distribution of galaxies $n_s^i(z)$ for the four tomographic bins for METACALIBRATION. The black line shows the CMB lensing kernel.

The precise range of scales impacted by the tSZ bias is dependent on the redshift bin of the source galaxies (see Fig. 4 of [23]). In contrast, the impact of baryons is maximal at the smallest scales, and typically negligible for separations beyond about 5 Mpc. Based on these results, it was demonstrated in [23] that the impact of the combination of these effects can be mitigated by excluding small scales from the analysis.

In this study we adopt the scale cuts directly from [23]. The scale cuts exclude angular bins below 40 arc min for the two lowest redshift bins, and scales below 60 arc min for the two highest redshift bins.⁵ These scale cuts are primarily driven by the tSZ bias; however, we emphasize that in the absence of tSZ bias, baryonic effects would still necessitate removal of a significant fraction of angular scales. Over the range of included angular scales, residual baryonic effects are expected to be negligible, while residual tSZ bias is nonvanishing. We quantify the impact of this residual bias in Sec. VC, showing that for the current level of measurement uncertainties, its impact on parameter constraints is small.

We note that the scale cut choices made in this analysis were motivated from consideration of the full 5×2 pt data vector, and not from consideration of $w^{\gamma_i \kappa_{\text{CMB}}}(\theta)$ alone. This choice was made because one of the main purposes of this work is to provide the measurements of $w^{\gamma_i \kappa_{\text{CMB}}}(\theta)$ that will be incorporated into the companion analysis of [24]. Since the other four two-point functions also contribute some

⁵These angular scale cuts are applied to the two-point correlation measurement between galaxy weak lensing and the CMB lensing map, not the temperature map that is used to reconstruct the lensing map.

potential bias in the 5×2 pt analysis, the scale cut choice adopted here is conservative for the analysis of $w^{\gamma_i \kappa_{\text{CMB}}}(\theta)$ alone.

V. MEASUREMENT

The measured two-point angular correlation functions, $w^{\gamma_i \kappa_{\text{CMB}}}(\theta)$, for each of the source galaxy bins are shown in Fig. 2. For each redshift bin we measure the correlation function in 10 angular bins logarithmically spaced between 2.5 and 250 arc min. We choose this binning to preserve

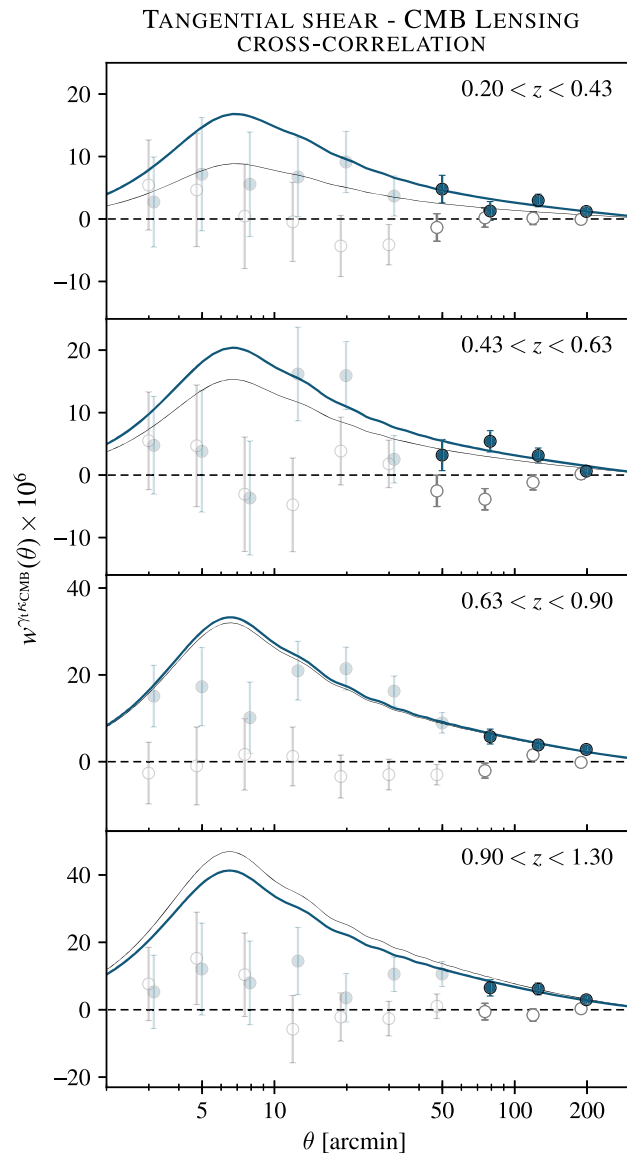


FIG. 2. Measurements of $w^{\gamma_i \kappa_{\text{CMB}}}(\theta)$ (filled circles) and $w^{\gamma_i \times \kappa_{\text{CMB}}}(\theta)$ (open circles) using METACALIBRATION shear estimates and the SPT+*Planck* CMB lensing map. The four panels show results for the four source galaxy redshift bin. Faded points are removed from the final analysis due to systematics or uncertainties in the modeling. Also shown are the theoretical predictions using fiducial cosmology with $A = 1$ (black curves), and with best-fit A (blue curves), where A is defined in Sec. VI A.

TABLE II. Results of the amplitude fitting analysis described in Sec. VI A, assuming *Planck* best-fit Λ CDM cosmology. Results shown correspond to METACALIBRATION measurements with angular scale cuts applied. The numbers enclosed in parentheses are fits for γ_{\times} to $A = 0$.

Sample	A	χ^2/ν	p.t.e.
$0.20 < z < 0.43$	1.90 ± 0.53	2.6/3 (0.4/4)	0.46 (0.98)
$0.43 < z < 0.63$	1.33 ± 0.36	2.9/3 (8.9/4)	0.41 (0.06)
$0.63 < z < 0.90$	1.04 ± 0.22	0.7/2 (4.3/3)	0.69 (0.23)
$0.90 < z < 1.30$	0.88 ± 0.20	1.0/2 (0.7/3)	0.60 (0.87)
All bins	0.99 ± 0.17	12.2/13 (6.9/14)	0.51 (0.94)

reasonable signal to noise in each angular bin, as discussed in [23].

A. Testing the measurements

1. Correlation of κ_{CMB} with γ_{\times}

When cross correlating the observed galaxy shears with the κ_{CMB} map, we divide the observed shear into a tangential component, γ_t , oriented tangentially to the line connecting the two points being correlated, and a cross component, γ_{\times} , which is 45° to the line connecting the two points. Weak lensing is expected to produce a tangential shear component only, and therefore the presence of a nonzero cross correlation with the cross-shear component would indicate the presence of systematic errors (such as errors in the point spread function (PSF) estimation, which will mix γ_t into γ_{\times}).

In Fig. 2, we show the measured cross correlation between the κ_{CMB} maps and the cross component of the shear (open points). As expected, we find that the measured cross correlation is consistent with zero in all redshift bins. We calculate the χ^2/ν (where ν is the number of degrees of freedom) and probability to exceed (p.t.e.) between the measurement and the null hypothesis (zero cross correlation) for all redshift bins combined, applying the angular scale cuts described in Sec. IV D, and find $\chi^2/\nu = 6.9/14$ and p.t.e. = 0.94, indicating consistency of the cross-shear correlation with zero. The χ^2/ν and p.t.e. for the individual bins are summarized in Table II.

B. Testing the covariance

As mentioned in Sec. IV B, we employ a theoretical covariance matrix (with a small empirical modification) when fitting the measured correlation functions. To test whether the theoretical covariance accurately describes the noise in the measurements, we compare it to an estimate of the covariance obtained using the “delete-one” jackknife method applied to data.

To compute the jackknife covariance estimate, we divide the source galaxy samples into $N_{\text{jk}} = 100$ approximately equal-area patches. The jackknife estimate of the covariance is then computed as

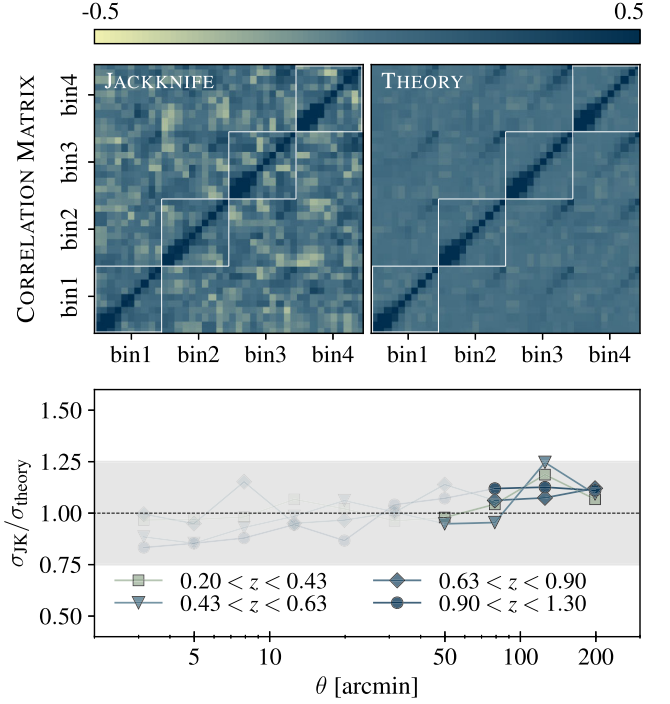


FIG. 3. The jackknife (upper left) and theory (upper right) correlation matrix ($C_{ij}/\sqrt{C_{ii}C_{jj}}$) for all the redshift bins. Lower panel: ratio of the diagonal component of the covariance matrix for the theory and the jackknife covariance in all redshift bins showing an agreement to within 25% (shown as the gray band) for all the redshift bins.

$$C_{ij}^{\text{jackknife}} = \frac{N_{\text{jk}} - 1}{N_{\text{jk}}} \sum_k (d_i^k - \bar{d}_i)(d_j^k - \bar{d}_j), \quad (12)$$

where d_i^k is the i th element of the $w^{\gamma_t \kappa_{\text{CMB}}}(\theta)$ data vector that is measured after excluding the shears in the i th patch on the sky and \bar{d} is

$$\bar{d}_i = \frac{1}{N_{\text{jk}}} \sum_k d_i^k. \quad (13)$$

We have validated the jackknife approach to estimating the covariance matrix of $w^{\gamma_t \kappa_{\text{CMB}}}(\theta)$ using simulated catalogs. The validation tests are described in Appendix B.

The theoretical and jackknife estimates of the covariance matrix, and the ratio between the diagonal elements of the two are shown in Fig. 3. It is clear from the top panels of the figure that the covariance structure of the theoretical covariance agrees qualitatively with the covariance measured from the data. Furthermore, the bottom panel shows that the two covariances agree along the diagonal to better than 25%⁶ across all redshift bins.

⁶Note that 25% is approximately the scatter we see when comparing the covariance computed from many FLASK (described in Appendix A) realizations and using the jackknife method on a single FLASK realization.

C. Estimating the impact of unmodeled systematics

While some sources of systematic error are modeled in the analysis (namely photometric redshift and multiplicative shear biases), there are several other potential sources of systematic errors coming from unmodeled effects that could impact the measurement of $w^{\gamma_t \kappa_{\text{CMB}}}(\theta)$. Some of these, such as tSZ bias, are minimized with angular scale cuts. One useful diagnostic to determine the impact of residual systematic biases is to identify the list of external quantities that could directly or indirectly contaminate the signal and cross correlate them with the measured galaxy shears and CMB convergence. We expect these cross correlations to be consistent with zero if these external quantities are not introducing significant biases in the measurements. One example of a quantity that could correlate both with observed shear and CMB convergence is dust extinction: dust extinction is lower at high galactic latitudes, which is where the density of stars is lowest, and therefore, could result in poor PSF modeling and biased shear estimates in those areas. Meanwhile, dust is one of the foreground components of the CMB temperature measurements, and one can expect potential residuals in a single frequency temperature map. When a contaminated temperature map is passed through the lensing reconstruction pipeline, fluctuations from these foregrounds get picked up as a false lensing signal, which will be spatially correlated with the variations in the galaxy shape measurements, and therefore introduce biases in our measurements.

We divide potential systematic contaminants into two categories: those that are expected to be correlated with the true (i.e., uncontaminated) γ or κ_{CMB} , and those that are not. For those systematics that are expected to be uncorrelated with the true γ and κ_{CMB} , we estimate the contamination of $w^{\gamma_t \kappa_{\text{CMB}}}(\theta)$ via

$$w_S(\theta) = \frac{w^{\kappa_{\text{CMB}}^{\text{obs}}} S(\theta) w^{\gamma_t^{\text{obs}}} S(\theta)}{w^{SS}(\theta)}, \quad (14)$$

where S is the foreground map of interest. This expression captures correlation of the systematic with both κ_{CMB} and γ , and is normalized to have the same units as $w^{\gamma_t \kappa_{\text{CMB}}}(\theta)$. Unless the systematic map is correlated with both γ_t and κ_{CMB} , it will not bias $w^{\gamma_t \kappa_{\text{CMB}}}(\theta)$ and $w_S(\theta)$ will be consistent with zero.

We consider three potential sources of systematic error that are expected to be uncorrelated with the true γ and κ_{CMB} : γ_t^{PSFres} (the residual PSF ellipticity), E_{B-V} (dust extinction), and δ_{star} (stellar number density). We use the difference between the PSF ellipticity between the truth (as measured from stars) and the model for the PSF residual. Descriptions of the E_{B-V} and δ_{star} maps can be found in [65]. The measured $w_S(\theta)$ for these quantities are plotted in Fig. 4 relative to the uncertainties on $w^{\gamma_t \kappa_{\text{CMB}}}(\theta)$. The error bars shown are determined by cross correlating the systematic maps with simulated κ_{CMB} , γ_t maps generated using

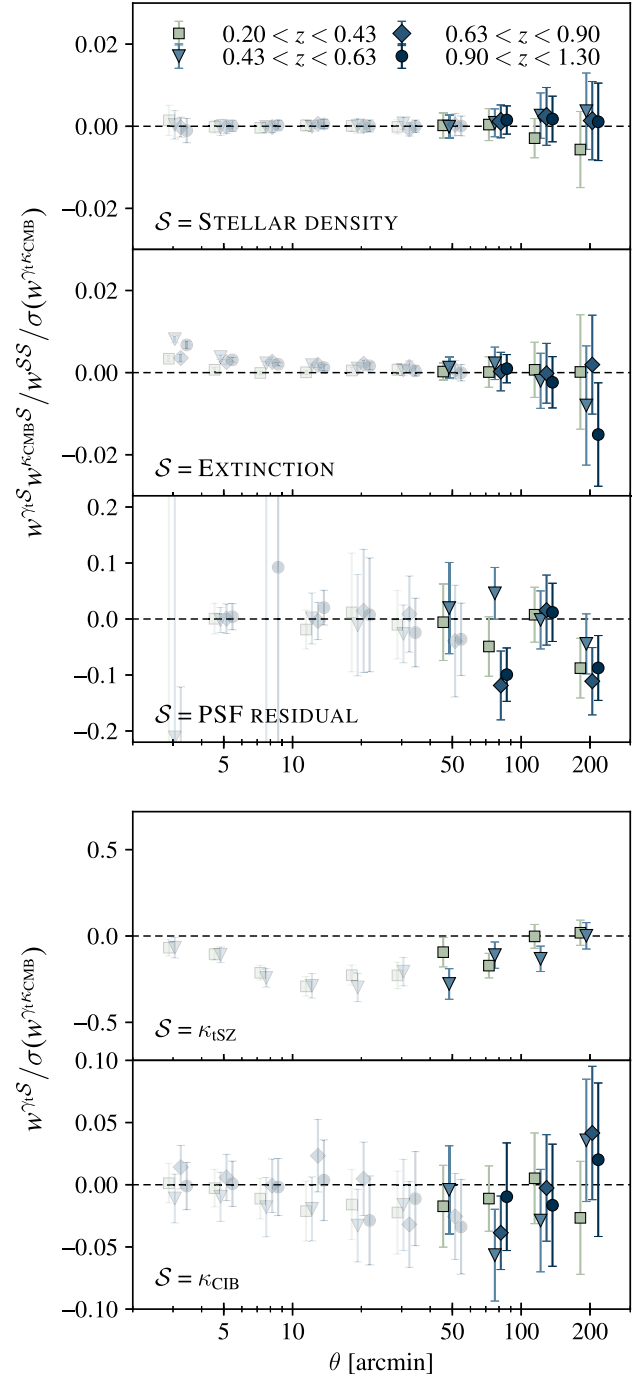


FIG. 4. Ratios of the estimated systematic biases to $\gamma_t \kappa_{\text{CMB}}$ from various contaminants to the statistical uncertainties on $\gamma_t \kappa_{\text{CMB}}$. We find that all systematics considered a result in negligible bias to the $\gamma_t \kappa_{\text{CMB}}$ measurements. For the case of PSF residuals, the auto-correlation $w^{SS}(\theta)$ of some bins are close to zero, resulting in large error bars for certain bins. As described in the text, contamination from the tSZ effect and the CIB (bottom two panels) must be treated somewhat differently from the other contaminants, since these two potential sources of bias are known to be correlated with the signal. While we find significant evidence for nonzero $w^{\gamma_t \kappa_{\text{CMB}}}(\theta)$, the size of this correlation is small compared to the error bars on $w^{\gamma_t \kappa_{\text{CMB}}}(\theta)$ and does not lead to significant biases in cosmological constraints.

the FLASK package [66]. For each of the potential systematics considered, we find that the measured $w_S(\theta)$ is much less than the statistical uncertainties on the $w^{\gamma, \kappa_{\text{CMB}}}(\theta)$ correlation, implying that there is very little impact from these systematics.

Astrophysical systematic effects that we expect to correlate with the true γ and κ_{CMB} must be treated somewhat differently, since in this case, Eq. (14) will not yield the expected bias in $w^{\gamma, \kappa_{\text{CMB}}}(\theta)$. Two sources of potential systematic error are expected to have this property, namely contamination of the κ_{CMB} map by tSZ and the CIB. Since the tSZ and CIB are both correlated with the matter density, these contaminants will be correlated with the true shear and κ_{CMB} signals. For both contaminants, we construct convergence maps of the contaminating fields across the DES patch, which we refer to as κ_{tSZ} and κ_{CIB} . The estimates of κ_{tSZ} and κ_{CIB} are generated as described in [23].

We estimate the bias induced to $w^{\gamma, \kappa_{\text{CMB}}}(\theta)$ by tSZ and CIB by measuring $w^{\gamma, \kappa_{\text{tSZ}}}(\theta)$ and $w^{\gamma, \kappa_{\text{CIB}}}(\theta)$. These quantities are plotted in Fig. 4, with error bars determined by measuring the variance between the systematic maps with 100 simulated sky realizations generated using the FLASK simulations (see Appendix A for details). We measure a bias over the angular ranges of interest, with a maximum bias⁷ of $\sim 0.30\sigma$ [where σ is the expected standard deviation for $w^{\gamma, \kappa_{\text{CMB}}}(\theta)$]. As shown in [23], this level of bias results in a small shift to inferred parameter constraints.

VI. PARAMETER CONSTRAINTS

We assume a Gaussian likelihood for the data vector of measured correlation functions, \vec{d} , given a model, \vec{m} , generated using the set of parameters \vec{p} :

$$\ln \mathcal{L}(\vec{d}|\vec{m}(\vec{p})) = -\frac{1}{2} \sum_{ij}^N (d_i - m_i(\vec{p})) \mathbf{C}_{ij}^{-1} (d_j - m_j(\vec{p})), \quad (15)$$

where the sums run over all of the N elements in the data and model vectors. The posterior on the model parameters can be calculated as

$$P(\vec{m}(\vec{p})|\vec{d}) \propto \mathcal{L}(\vec{d}|\vec{m}(\vec{p})) P_{\text{prior}}(\vec{p}), \quad (16)$$

where $P_{\text{prior}}(\vec{p})$ is the prior on the model parameters.

In the following sections, we will use this framework to generate parameter constraints in four scenarios, each keeping different sets of parameters free.

⁷Reference [23] uses theory data vectors and model fits to the measured biases to calculate similar quantities, from which the scale cuts are derived. In contrast, the measurements shown in Fig. 4 are calculated using the κ_{tSZ} map and the galaxy shape catalogs, and therefore includes scatter. Although it may appear as though the scale cuts are removing less biased angular bins, this is primarily due to the scatter in our measurements.

We note that we made minor modifications to the analysis after we unblinded the data. We originally computed the constraints on shear calibration and intrinsic alignment parameters fixing the cosmology to the values obtained from DES-Y1 in Secs. VIB and VIC. We later allowed the cosmological parameters to vary but combined with the *Planck* baseline likelihood. Consequently, we also switched to using models generated assuming *Planck* best-fit values when fitting the correlation amplitudes in Sec. VIA, so that the same framework is used throughout the analysis.

A. Amplitude fits

We first attempt to constrain the amplitude of the observed correlation functions relative to the expectation for the fiducial cosmological model summarized in Table I. The fiducial cosmological parameters are chosen to be the best-fitting parameters from the analysis of CMB and external datasets in [60]; and nuisance parameter values (shear calibration bias, intrinsic alignment and source redshift bias) are chosen to be the best-fitting parameters from the analysis of [12]. In this case, the model is given by $\vec{d} = A\vec{d}_{\text{fid}}$, where A is an amplitude parameter and \vec{d}_{fid} is the model for the correlation functions computed using the fiducial cosmological model of Table I. The model is computed as described in Sec. IV B.

The resultant constraints on A for each redshift bin (and for the total data vector) are summarized in Table II. We find that the measured amplitudes are consistent with $A = 1$, although the first redshift bin is marginally high. We calculate the p.t.e. using the χ^2 of the measurement fit to the fiducial model with $A = 1$ and obtain 0.14, which suggests that this deviation is not significant. We additionally note the mild correlation between A and redshift, although with our uncertainties, no conclusions could be made.

The constraint on A using all redshift bins is $A = 0.99 \pm 0.17$. Furthermore, the resultant χ^2 and p.t.e. values indicate that the model is a good description of the data. These values are shown in the rightmost columns of Table II. This measurement rejects the hypothesis of no lensing at a significance of 6.8σ , and the best fit model is preferred over the no-lensing model at 5.8σ .⁸ The latter value can be compared directly with results from past work: the cross-correlation measurement between Canada-France-Hawaii telescope stripe-82 survey and Atacama Cosmology Telescope obtained 4.2σ [14], RCSLenS and *Planck* obtained 4.2σ [19], DES-SV and SPT-SZ obtained 2.9σ [18], and KiDS-450 and *Planck* obtained 4.6σ [20]. We also estimate the detection significance and signal-to-noise ratio we would have obtained with no scale cuts and

⁸The two values are calculated using $\sqrt{\chi_{\text{null}}^2}$ and $\sqrt{\chi_{\text{null}}^2 - \chi_{\text{min}}^2}$, respectively.

TABLE III. Constraints on m^i from combining $\gamma_{t\kappa_{\text{CMB}}}$ and $\gamma\gamma$ with the *Planck* baseline likelihood. The constraints we obtain here are weaker than those obtained through other simulation and data based calibration methods described in [37].

Sample	$\gamma_{t\kappa_{\text{CMB}}}$	$\gamma\gamma$
$0.20 < z < 0.43$...	$0.02^{+0.15}_{-0.16}$
$0.43 < z < 0.63$	$-0.08^{+0.47}_{-0.31}$	$-0.04^{+0.09}_{-0.10}$
$0.63 < z < 0.90$	$-0.06^{+0.20}_{-0.28}$	$-0.10^{+0.05}_{-0.05}$
$0.90 < z < 1.30$	$-0.14^{+0.14}_{-0.28}$	$-0.05^{+0.06}_{-0.06}$

find 10.8 and 8.2σ , respectively. (We note that biases due to tSZ and baryonic effects both tend to lower the cross-correlation amplitude; hence, these values are underestimates of the detection significance we would have found in the absence of these biases.)

B. Constraining shear calibration bias

In this section and Sec. VI C, we marginalize over the cosmological parameters and nuisance parameters (shear calibration bias, intrinsic alignment, and source redshift bias) simultaneously over the ranges given in Table I but combine our measurements with the *Planck* baseline likelihood.⁹ In addition, instead of applying Gaussian priors on the shear calibration biases, we vary them over the range $[-1, 1]$ and evaluate the constraining power that $w^{\gamma_{t\kappa_{\text{CMB}}}}(\theta)$ has on these parameters.

From this, we obtain $m^{2,3,4} = [-0.08^{+0.47}_{-0.31}, -0.06^{+0.20}_{-0.28}, -0.14^{+0.14}_{-0.28}]$. The data do not constrain m^1 well (i.e., the constraint is prior dominated), which could be explained by the small overlap between the CMB lensing and the galaxy lensing kernel for this bin. These results are consistent with the constraints from cosmic shear measurements when the parameters are marginalized over in the same way: $m^{1,2,3,4} = [0.02^{+0.15}_{-0.16}, -0.04^{+0.09}_{-0.10}, -0.10^{+0.05}_{-0.05}, -0.05^{+0.06}_{-0.06}]$, but significantly weaker than the imposed priors in [12], which point to best-fit values of $0.012^{+0.023}_{-0.023}$ for all the bins. These results are summarized in Table III, and the posterior distributions are shown in Fig. 5. Our analysis demonstrates the potential of using cross-correlation measurements between galaxy lensing and CMB lensing to constrain shear calibration bias. However, to reach the level of DES priors, the signal to noise of the galaxy-CMB lensing cross correlations would have to improve by a factor of approximately 30.

C. Constraining intrinsic alignment parameters

Using the same framework as Sec. VI B we attempt to constrain the nonlinear alignment model parameters A_{IA} and η_{IA} . For the amplitude, we obtain $A_{\text{IA}} = 0.54^{+0.92}_{-1.18}$,

⁹Here we use the combination of low- ℓ TEB and high- ℓ TT likelihoods.

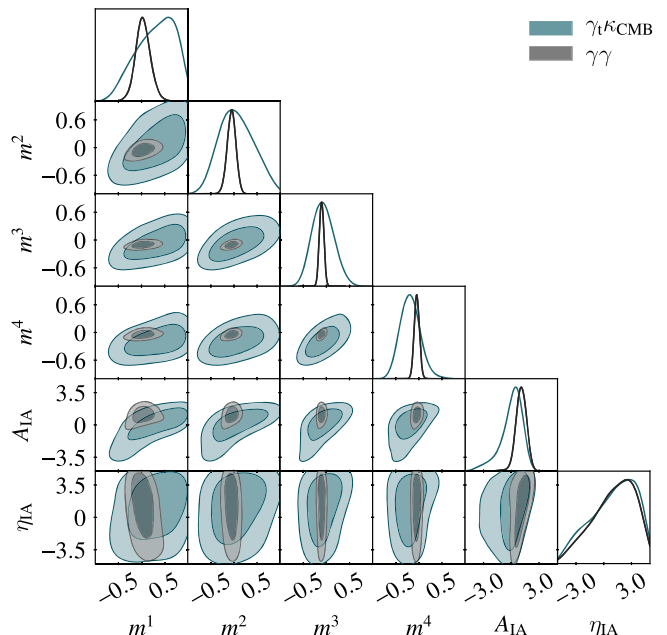


FIG. 5. Constraints on m^i , A_{IA} , and η_{IA} that we marginalize over (source redshift bias parameters are also marginalized over but not shown here). The constraints that we obtain are weaker but in agreement with that from the DES cosmic shear measurements [11].

which can be compared to $A_{\text{IA}} = 1.02^{+0.64}_{-0.52}$, obtained from the DES-Y1 cosmic shear measurements. These results are in agreement with each other, although it is noted that the values are not well constrained. Since the product of galaxy weak lensing and CMB lensing kernels span a wider redshift range compared to the galaxy weak lensing kernel alone, we might expect to obtain a better constraint on the redshift evolution parameter η_{IA} using $\gamma_{t\kappa_{\text{CMB}}}$ correlations over $\gamma\gamma$. However, due to the noise level of the CMB lensing map used in this analysis, we find no significant constraint on this parameter. The results are shown in Fig. 5 and are summarized in Table IV.

D. Cosmological parameter fits

The lensing cross-correlation measurements should be sensitive to the information about the underlying dark-matter distribution and the growth of dark-matter structure in the universe, and hence should be sensitive to Ω_{m} and $S_8 \equiv \sigma_8 \sqrt{(\Omega_{\text{m}}/0.3)}$. The constraints that we obtain on

TABLE IV. Constraints on A_{IA} assuming the nonlinear alignment model, when combining our $w^{\gamma_{t\kappa_{\text{CMB}}}}(\theta)$ measurement and the *Planck* baseline likelihood.

Probe	A_{IA}
$\gamma_{t\kappa_{\text{CMB}}}$	$0.54^{+0.92}_{-1.18}$
$\gamma\gamma$	$1.02^{+0.64}_{-0.52}$

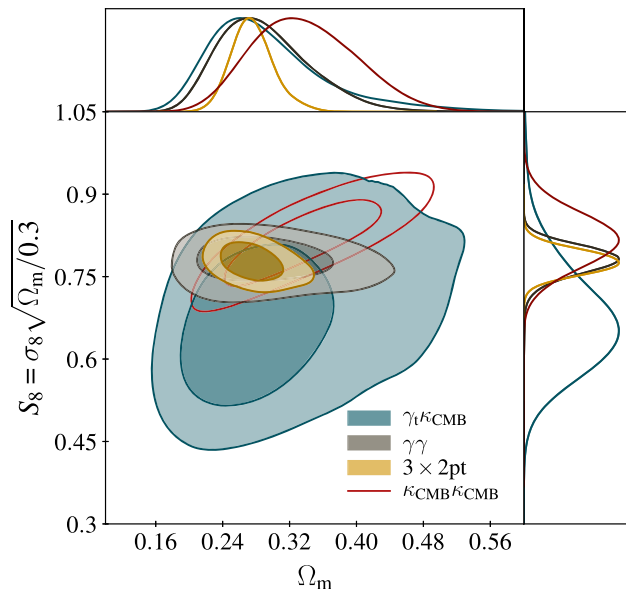


FIG. 6. Constraints on Ω_m and S_8 from $\gamma_t \kappa_{\text{CMB}}$, DES cosmic shear measurement [11], DES 3×2 pt measurement [12], and *Planck* $\kappa_{\text{CMB}} \kappa_{\text{CMB}}$ measurement [9].

these parameters are shown in Fig. 6 and are compared with the ones obtained from the DES-Y1 cosmic shear results [11], DES-Y1 joint analysis [12], and CMB lensing alone [10]. The comparison between our results and that of cosmic shear is interesting since we are essentially replacing one of the source planes in [11] with the CMB. We find that the constraints that we obtain for $w^{\gamma_t \kappa_{\text{CMB}}}(\theta)$ are less constraining than but consistent with the cosmic shear results. The marginalized constraints on Ω_m and S_8 are found to be $0.261^{+0.070}_{-0.051}$ and $0.660^{+0.085}_{-0.100}$, respectively, whereas [11] finds $\Omega_m = 0.260^{+0.065}_{-0.037}$ and $S_8 = 0.782^{+0.027}_{-0.027}$.

VII. CONCLUSIONS

We have presented a measurement of the cross correlation between galaxy lensing as measured by DES and CMB lensing as measured by SPT and *Planck*. The galaxy lensing measurements are derived from observed distortions of the images of galaxies in approximately the redshift range of $0.2 < z < 1.3$; the CMB lensing measurements, on the other hand, are inferred from distortions of the CMB temperature map induced by intervening matter along the line of sight of photons traveling from the last scattering surface.

The cross correlation is detected at 8.2σ significance including all angular bins; this is reduced to 5.8σ after removing scales that we find to be affected by systematics such as tSZ contamination of κ_{CMB} and the effects of baryons on the matter power spectrum as described in [23].

We perform several consistency checks on the measurements as well as tests for possible systematic errors. These include performing null tests by cross correlating κ_{CMB} with stellar density, dust extinction, PSF residuals, and the

cross-shear component, and testing our model for tSZ and CIB contamination of the κ_{CMB} map. We find that of these possible systematics, the tSZ effect dominates, and we mitigate this bias by applying scale cuts to remove the angular scales that are affected the most.

The analytical covariance matrix that we use is tested by comparing with the jackknife covariance matrix estimated directly from the data. The diagonal elements of these covariance matrices agree to within 25%, which is a reasonable agreement given that the jackknife method produces a noisy estimate of the underlying covariance.

Using the measured $w^{\gamma_t \kappa_{\text{CMB}}}(\theta)$ correlation functions, we perform parametric fits. Assuming a Λ CDM *Planck* best-fit cosmology and fixing nuisance parameters to fiducial values set by DES-Y1, we obtain a global best-fit amplitude of $A = 0.99 \pm 0.17$ which is consistent with expectations from the Λ CDM cosmological model ($A = 1$).

Next, we combine our measurement with the *Planck* baseline likelihood, vary the nuisance parameters, and attempt to constrain them. For the shear calibration bias parameters we obtain the constraints $m^{2,3,4} = [-0.08^{+0.47}_{-0.31}, -0.06^{+0.20}_{-0.28}, -0.14^{+0.14}_{-0.28}]$, while m^1 is not constrained well. These constraints are less stringent than the DES-Y1 priors derived from data and simulations, and it is anticipated that the $\gamma_t \kappa_{\text{CMB}}$ correlation will be able to constrain shear calibration bias to better precision than these methods [67] for future surveys such as CMB-S4 [68] and LSST [69].

For the amplitude of IA, we obtain the constraint $A_{\text{IA}} = 0.54^{+0.92}_{-1.18}$, which is in agreement with what is obtained from DES-Y1 cosmic shear measurements. However, the redshift evolution parameter η_{IA} is not constrained well using $w^{\gamma_t \kappa_{\text{CMB}}}(\theta)$ measurement alone.

When we marginalize over the nuisance parameters using the DES-Y1 priors listed in Table I, we obtain constraints on cosmological parameters that are consistent with recent results from [37]: $\Omega_m = 0.261^{+0.070}_{-0.051}$ and $S_8 \equiv \sigma_8 \sqrt{\Omega_m / 0.3} = 0.660^{+0.085}_{-0.100}$. While the constraining power of $\gamma_t \kappa_{\text{CMB}}$ is relatively weak, we obtain independent constraints on Ω_m and S_8 , which will help break degeneracies in parameter space when all the probes are combined.

Future data from the full DES survey and SPT-3G [70] should provide significant reduction in measurement uncertainties on the $w^{\gamma_t \kappa_{\text{CMB}}}(\theta)$ correlation function. For SPT-3G, the CMB lensing map will be reconstructed using polarization data, which will have minimal foreground biases.¹⁰ With these potential improvements, the $\gamma_t \kappa_{\text{CMB}}$ cross correlation is a promising probe from which it will be used to extract constraints independent of those from galaxy shear or CMB measurements alone.

¹⁰Temperature based lensing reconstruction will be carried out using methods outlined in [71,72], such that the resulting map is less sensitive to foreground biases.

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APPENDIX A: FLASK SIMULATIONS

In this work, we make use of the publicly available code FLASK [66] to generate correlated maps between shear and CMB lensing. We use FLASK to generate 120 full-sky log-normal realizations of the density field and four galaxy shear maps corresponding to the four redshift bins we use for the data. Additionally, we generate a convergence map at $z = 1089$, and we treat this as a noiseless CMB convergence map. The galaxy shear catalogs are generated using galaxy number densities and shape noise measured from data, and Gaussian noise realizations generated from

the noise power spectrum of the CMB convergence maps are added to the noiseless convergence map to produce datalike catalogs and maps. For each full sky simulation, we extract out ten subcatalogs by applying the DES-Y1 angular mask, resulting in 1200 synthetic galaxy shear catalogs and CMB convergence maps that have noise properties matched to the real data.

APPENDIX B: VALIDATION OF JACKKNIFE COVARIANCE ESTIMATE

To test whether the jackknife covariance estimate provides a reliable estimate of the true covariance over the scales considered, we make use of FLASK simulation realizations. For each of the simulated catalogues, we measure $w^{\gamma, \kappa_{\text{CMB}}}(\theta)$ using the same procedure as applied to the real data. We then compute the covariance matrix directly across the 1200 simulated catalogs, which provides a low-noise estimate of the covariance of $w^{\gamma, \kappa_{\text{CMB}}}(\theta)$ in the FLASK simulations (which we call “true” FLASK covariance). From the simulated catalogue, we also compute the jackknife estimate of the covariance and compare this with the true FLASK covariance. We find that these are consistent with each other to within 25%.

¹¹<https://bitbucket.org/joezuntz/cosmosis>.

¹²<https://getdist.readthedocs.io/en/latest/>.

¹³<https://github.com/dhanson/quicklens>.

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