

Accurate determination of the specific absorption rate in superparamagnetic nanoparticles under non-adiabatic conditions

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We report on a general description of non-adiabatic calorimetry measurements for improving the accuracy on the determination of the specific absorption rate of superparamagnetic nanoparticles subjected to alternating magnetic fields. We perform experiments on reduced volumes of iron oxide nanoparticles dispersed in aqueous media under different thermal equilibrium conditions. We introduce a simple model, which considers linear thermal losses to precisely reproduce the complete time evolution of temperature. The control and the quantification of heat losses lead to higher accuracy for determining the specific absorption rate in superparamagnetic nanoparticles.

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Superparamagnetic iron oxide nanoparticles (SPION) are of great interest for biomedical applications because of their suitable magnetic, colloidal, and structural properties. Different chemical synthesis methods allow to produce SPION with distinct biocompatible coatings,¹ controlled aggregate size, and high colloidal stability.² SPION have shown potential applications as contrast agents,³ drug delivery nanocarriers,⁴ and local heating inductors.⁵ For the latter applications, the iron mass-normalized specific absorption rate (SAR)⁵ is the commonly used physical magnitude for evaluating the calorific power of SPION subjected to alternating magnetic fields (H_{AC}). SAR is determined by standard calorimetric methods⁶ according to the expression $SAR = C/mdT/dt|_{t=0}$, where C is the specific heat capacity of the sample, m is the iron mass of magnetic material in solution, and $dT/dt|_{t=0}$ is the slope of the temperature increase at initial times after applying H_{AC} . An accurate determination of SAR is hence essential for quantifying the magnetic heating power of SPION for their application as intracellular hyperthermia generators.

SPION SAR values tightly depend on nanoparticle parameters such as size^{7,8} or concentration,^{9,11} or sample volume,¹² nanoparticle interactions¹⁰ and alternating magnetic field parameters such as frequency, amplitude,^{7,13} or field inhomogeneities.¹² Adiabatic or non-adiabatic experimental conditions have also a strong influence in the SAR quantification.¹⁴ Adiabatic conditions provide more accurate SAR values than those obtained under non-adiabatic ones. The latter always requires the performance of calorimetry measurements under thermal equilibrium conditions in order to extract the right value of $dT/dt|_{t=0}$ necessary for SAR determination. In this manner, the $dT/dt|_{t=0}$ value will be scarcely influenced by thermal losses of SPION into the surrounding via radiative, convection, and conduction mechanisms.¹⁵ However, non-adiabatic conditions provide a more realistic scenario for applying the intracellular magnetic heating

power of SPION in both *in vitro*¹⁶ and *in vivo*¹⁷ studies. Thus, the control and the quantification of SPION thermal losses with the surrounding are required to determine SAR values with higher accuracy.

The purpose of this letter is to provide a general description of non-adiabatic calorimetry measurements performed on reduced volumes of SPION (tens of μ l) subjected to H_{AC} in order to quantify more accurately their SAR value. We have carried out experiments at different equilibrium temperatures (T_{eq}) in the range from 10 °C to 30 °C and applying H_{AC} under different equilibrium conditions. We propose a simple model to reproduce the time variation of SPION temperature when H_{AC} is turned on and off. The model is based on the linear heat losses of SPION into the surrounding. Our experimental findings point out the advantage of performing calorimetry measurements on reduced SPION volumes in order to determine more accurate SAR values.

Fe₃O₄ SPION were synthesized by modification of previously described thermal decomposition procedure of an iron complex precursor.¹⁸ SPION were then coated with dimercaptosuccinic acid (DMSA) by a ligand exchange process^{19,20} in order to disperse them in aqueous media. The SPION core size (18 nm, standard deviation 2 nm) was determined by transmission electron microscopy while their hydrodynamic diameter in water dispersions (65 nm, Polydispersity index = 0.18) was measured through dynamic light scattering. The colloidal suspension stability of our DMSA coated SPION dispersed in water was extremely high. No SPION sedimentation was observed for months or even after applying H_{AC} for hours leading to high reproducibility of the calorimetry measurements. Thermal measurements were performed in a home-made set-up of reduced volume (up to 40 μ l). For such reduced volume, we can assume a constant temperature into the solution. The sample holder is a glass flask with a vacuum shield covered by a polystyrene stopper where an upper aperture allows to introduce the temperature

probe. This aperture is responsible for the thermal exchange of the sample with the surroundings (lab environment) via convection mechanisms. H_{AC} up to 250 kHz and 50 mT are generated by a home-made air-cooled ferrite core, coiled with Litz wires, which is part of a LCR resonant circuit. The SPION temperature was measured with a commercial optical fibre probe TS2/2 connected to a FOTEMP2-16 two-channel signal conditioner from Optocon AG with an experimental error of $\pm 0.2^\circ\text{C}$. For the present study, calorimetry measurements have been performed on a 35 μl volume of SPION dispersed in distilled water with an iron concentration of 10 g/l. SPION were subjected to the same given H_{AC} conditions (78 kHz and 25 mT during 8 min) for different initial temperatures (T_i) and T_{eq} in the range from 10°C to 30°C .

Figure 1 compares calorimetry measurements recorded at slightly different T_{eq} . At first glance, a similar behaviour of temperature variation is observed: a sudden SPION temperature increase (thin line) when H_{AC} is on due to the magnetically induced heating of SPION followed by a progressive temperature saturation. Finally, SPION temperature decays (thick line) when H_{AC} is turned off due to SPION heat losses into the surrounding. Under non-adiabatic conditions, the saturation temperature (T_{sat}) is related to a thermal equilibrium reached when the SPION heat losses compensate the magnetic heating power. Fig. 1(a) shows the temperature variation of two consecutive measurements when H_{AC} is turned on at $T_i = T_{eq,1} = 30.2^\circ\text{C}$, i.e., under equilibrium conditions. Within experimental error, the different measurement trials show a reproducibility better than 99%. In turn, Fig. 1(b) shows the SPION temperature variation when H_{AC} is turned on at different T_i for $T_{eq,2} = 28.4^\circ\text{C}$. Note that the measurements starting at $T_i > T_{eq,2}$ are performed under thermal non-equilibrium conditions. Thus, the temperature increment (ΔT) has similar values of $\approx 10^\circ\text{C}$ under thermal equilibrium conditions (i.e., when $T_i = T_{eq}$), whilst

$\Delta T < 10^\circ\text{C}$ when $T_i > T_{eq}$. As mentioned below, this will have also relevant implications on the value of $dT/dt|_{t=0}$.

A first quantitative SAR analysis can be derived when numerically differentiating the temperature curves (see Figs. 1(c) and 1(d)). In general, SAR value is determined from the temperature increase at initial times immediately after turning H_{AC} on, i.e., $dT/dt|_{t=0}$. In practice, the conventional procedure currently employed for determining SAR values is based on quantifying the maximum value of $dT/dt(t)$ at initial times, i.e., $dT/dt|_{\max}$.

Fig. 1(c) shows the derivative of the temperature variation plotted in Fig. 1(a). One can observe identical positive and negative dT/dt behaviour under thermal equilibrium conditions at $T_{eq,1}$. The maximum and minimum values of dT/dt have an identical absolute value of $|dT/dt|_{\max/\min} = 0.11\text{ K/s}$ (see solid circles in Fig. 1(c)). Contrary, a different dT/dt behavior is observed under thermal non-equilibrium conditions (i.e., $T_i > T_{eq}$). Fig. 1(d) shows the derivative curve of the temperature variation shown in Fig. 1(b). As one can see, while the negative part of dT/dt reaches similar minimum values along the whole time span, the maximum values of dT/dt decrease when increasing the difference between T_i and T_{eq} . This fact stresses that SPION SAR values are properly defined only when calorimetry measurements are performed under thermal equilibrium, otherwise SAR values are underestimated.

In case of our calorimetry measurements, these equilibrium conditions are equally found when H_{AC} is turned on and off at temperatures T_{eq} and T_{sat} , respectively. In the first case, the SPION temperature variation at initial times immediately after applying H_{AC} is mainly influenced by the magnetically induced heating power of SPION and scarcely by heat transfer losses.¹⁴ In the second case, the SPION temperature variation is influenced by the vanishing of the magnetically induced heating power when turning H_{AC} off. In both cases, the heat transfer losses of SPION into the surrounding are the same. Hence, similar analysis than in case of turning H_{AC} on can be performed when H_{AC} is turned off, independently of the heat losses mechanisms involved. As shown in Figs. 1(c) and 1(d), identical values of $dT/dt|_{\min} = -0.11\text{ K/s}$ are observed. Thus, SAR can be equally determined under thermal equilibrium conditions by considering the initial rise or decay slope immediately after turning H_{AC} on or off, respectively, leading to the value of 46 W/g .

On the other hand, the conventional procedure involves some accuracy drawbacks. First, a linear fitting of the temperature slope immediately after applying H_{AC} is commonly established considering the same time interval and number of points (in our case 20 s and 20 points) and the experimental error of the temperature measurement ($\pm 0.2^\circ\text{C}$). In the precedent analysis, under equilibrium conditions the slope reads $0.11 \pm 0.01\text{ K/s}$, leading to $\text{SAR} = 46 \pm 4\text{ W/g}$ (10% relative inaccuracy). However, the absolute error is independent of the slope value, which may results in huge relative inaccuracies for small SAR values. Second, the heat transfer losses at initial times after applying H_{AC} lead to further inaccuracies. Both uncertainty sources can be properly considered when evaluating the heat loss mechanisms along the whole temperature variation curve, instead of the initial times only.

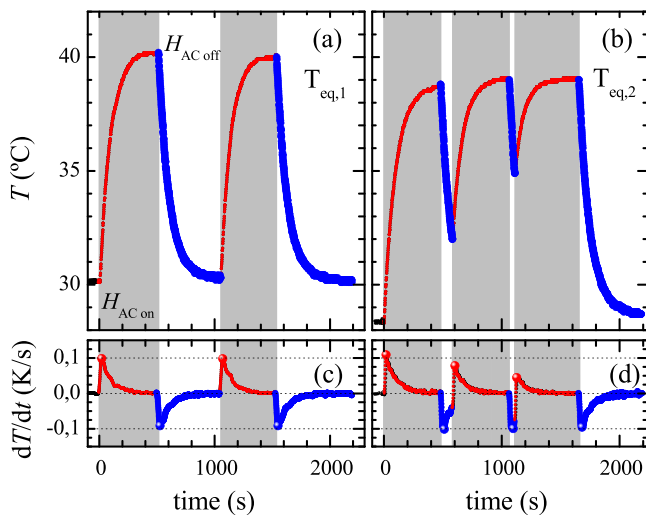


FIG. 1. Time evolution of SPION temperature when subjected to H_{AC} (78 kHz and 25 mT) (a) at $T_{eq,1} = 30.2^\circ\text{C}$, (b) at $T_{eq,2} = 28.4^\circ\text{C}$ for different T_i when applying H_{AC} . (c) and (d) Numerical derivative curves of data shown in (a) and (b), respectively. Shadow and white time zones are exposed to H_{AC} on and off, respectively. Thin and thick lines correspond to temperature rise and decay. Solid circles in (c) and (d) indicate the maximum and minimum dT/dt values.

In order to improve the accuracy on determining the SPION SAR values under non-adiabatic conditions, we propose a simple model based on linear heat losses of SPION. We assume that convection mechanism is the only heat transfer of SPION into the surrounding. The reduced SPION volume and the thermal insulation of the glass flask lead to negligible conduction and radiation losses. Later on, experimental data will confirm this assumption. Thus, from a simple convection rate equation,¹⁵ we can derive solutions for T_{rise} and T_{decay} whose expressions read:

$$\begin{aligned} T_{\text{rise}}(t) &= T_{\text{eq}} + \Delta T(1 - e^{-a(t-t_{\text{on}})}) \\ T_{\text{decay}}(t) &= T_{\text{sat}} - \Delta T(1 - e^{-a(t-t_{\text{off}})}), \end{aligned} \quad (1)$$

where $\Delta T = T_{\text{sat}} - T_{\text{eq}}$, $a = k/C$, k is the heat exchange of SPION into the surrounding, C is the specific heat of the sample, t_{on} and t_{off} are the times when H_{AC} is turned on and off, respectively. Notice that T_{rise} and T_{decay} have a similar but inverted time dependence. Our model has a single fitting parameter, namely a since T_{eq} and T_{sat} , and consequently ΔT , are determined from experimental data. Hence, the numerical value of $dT/dt|_{t=t_{\text{on/off}}} = \Delta T \cdot a$. The uncertainty of the numerical value of $dT/dt|_{t=t_{\text{on/off}}}$ can be now determined by Gaussian error propagation, which is a valid method for providing an interval of confidence to the numerical results derived from Eqs. (1). Now, SAR accuracy depends on the values and inaccuracies of ΔT and a , and is tested in larger number of points and time interval than the conventional procedure mentioned above.

Figure 2 compares the experimental data plotted at Figs. 1(a) and 1(b) with the fitting curves obtained from Eqs. (1) in order to calculate the temperature increase and decay when H_{AC} is turned on and off, respectively. The model is in good agreement with experimental results, being able to completely reproduce calorimetry measurements starting at $T_i > T_{\text{eq}}$. The fitting parameter value employed is $a = 0.0110 \pm 0.0005 \text{ s}^{-1}$. Note that now the relative SAR uncertainties are smaller than 5% what represents a significant increase of accuracy with respect to the conventional procedure (i.e., $\text{SAR} = 46 \pm 2 \text{ W/g}$).

In order to verify the validity of our assumptions on heat loss linearity, we perform experiments at $T_{\text{eq},3} = 10.0^\circ\text{C}$,

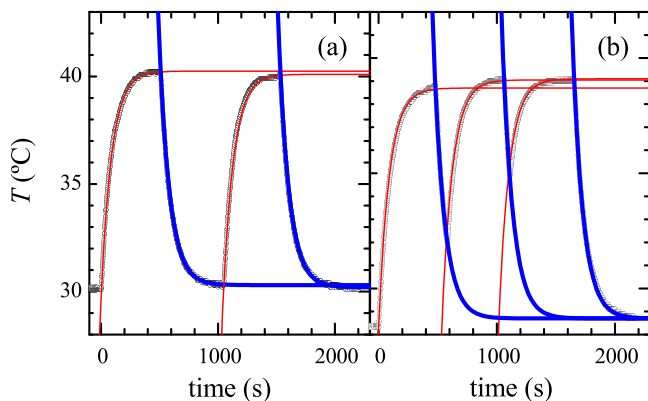


FIG. 2. Comparison of simulations and experimental data at (a) $T_{\text{eq},1} = 30.2^\circ\text{C}$ and (b) $T_{\text{eq},2} = 28.4^\circ\text{C}$. Circles correspond to experimental data, thin and thick lines correspond to numerical simulations obtained from Eqs. (1), with the fitting parameter $a = 0.0110 \pm 0.0005 \text{ s}^{-1}$.

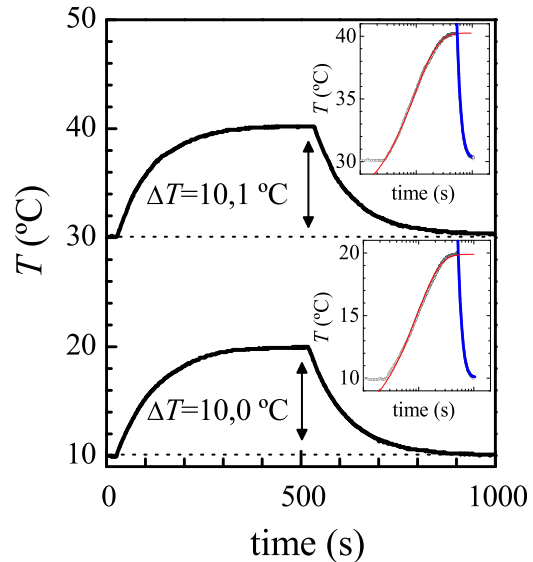


FIG. 3. Time evolutions of SPION temperature at $T_{\text{eq},1} = 30.2^\circ\text{C}$ and $T_{\text{eq},3} = 10.0^\circ\text{C}$ when subjected to H_{AC} (78 kHz and 25 mT). Insets: Comparison of numerical simulations and experimental data. Circles correspond to experimental data, thin and thick lines correspond to the numerical simulations obtained by using Eqs. (1), with the fitting parameter $a = 0.0110 \pm 0.0005 \text{ s}^{-1}$.

i.e., a temperature 20°C lower than previously. Figure 3 compares calorimetry measurements performed at $T_{\text{eq},1} = 30.2^\circ\text{C}$ and $T_{\text{eq},3} = 10.0^\circ\text{C}$. Identical temperature behaviour with a similar ΔT values than at higher temperatures T_{eq} are observed at both equilibrium temperatures. This indicates that the SPION thermal losses by radiation mechanism (proportional to $T^4 - T_{\text{eq}}^4$) are negligible in the studied temperature range (from 10°C to 30°C). This finding justifies the assumption of linear heat losses. Hence, the only heat transfer losses in our experimental systems may correspond to convection mechanisms as initially assumed. In fact, as shown in insets of Fig. 3, model calculations using the same fitting parameter value highly agree with the experimental results leading to similar SAR values within the studied temperature range.

In summary, we have studied the temperature variation of SPION subjected to H_{AC} under non-adiabatic conditions. Our experimental results show similar temperature variation curves for given H_{AC} conditions at different T_{eq} ranging from 10°C to 30°C . The use of reduced volumes of SPION water dispersions allows to precisely simulate calorimetry measurements by a simple model that considers the linearity of SPION heat losses into the surrounding. The control and the quantification of heat losses lead to higher accuracy in determining SAR values, for example, to disentangle the influence of the intrinsic SPION parameters (i.e., particle size or concentration) as well as extrinsic ones (i.e., H_{AC} conditions) on the SAR values. The proposed thermal description will remarkably improve the accuracy on the quantification of the thermal transfer induced by SPION for optimizing the efficiency of the magnetic heating.

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